

1 **Unbend: Correction of local beam-induced sample**
2 **motion in cryo-EM images using a 3D spline model**
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5 Lingli Kong,^{1*} Ximena Zottig,^{1,2} Johannes Elferich,^{1,2} Nikolaus Grigorieff^{1,2*}
6

7 ¹RNA Therapeutics Institute, University of Massachusetts Chan Medical School, Worcester, MA,
8 United States

9 ²Howard Hughes Medical Institute, University of Massachusetts Chan Medical School,
10 Worcester, MA, United States
11

12 *Correspondence: lingli.kong1@umassmed.edu, niko@grigorieff.org
13

14 **Abstract**

15 The exposure of frozen biological samples to the high-energy electron beam in a cryo-
16 electron microscope commonly leads to beam-induced sample motion and distortions. Previously,
17 we described *Unblur*, which is part of our *cisTEM* software to correct for beam-induced motion
18 based on the alignment of full frames in a movie collected during the beam exposure (Grant et al.,
19 2015). However, *Unblur* cannot accommodate motion due to more localized sample bending and
20 distortions. Here, we present *Unbend*, extending *Unblur* by incorporating local motion correction
21 using a three-dimensional cubic spline model. The 3D spline model is constructed using cubic B-
22 splines along the exposure time axis, and bicubic B-splines within movie frames. *Unbend* is
23 integrated into our *cisTEM* software with a new local motion visualization panel within the
24 *cisTEM* graphical user interface. We processed movie frames from various *in-situ* sample types,
25 including whole cells, lamellae, and cell lysates, to analyze motion behavior across different
26 specimen types. To quantify the improvement in high-resolution signal, we utilized the 2D
27 template matching method, which operates independently of the motion correction process, to
28 search large ribosomal subunits from the motion-corrected micrographs. Overall, the signal-to-
29 noise ratio of detected particles improved by 3–8% across different samples compared with full-
30 frame aligned micrographs, while the number of detected target particles increased by up to
31 ~300%. The total and Von Mises equivalent strain shows a deformation scale of less than 1% in
32 most of the samples, confirming that our model induces minimal additional distortion.
33 Furthermore, we processed micrograph montages to study motion patterns across an entire
34 sample, revealing considerable variance in distortion scale within the same sample, suggesting a
35 complex underlying mechanism.

36 **Introduction**

37 Cryo-electron microscopy (cryo-EM) enables structural biologists to observe diverse
38 biomolecules in their native environment. The molecules are preserved in amorphous ice, and in
39 the most favorable cases, their 3D structure can be reconstructed at near-atomic resolution. An
40 important factor determining the attainable resolution are high-quality micrographs, containing
41 high-resolution signal of the molecules. This high-resolution signal is attenuated by radiation
42 damage and sample motion during the exposure (beam-induced motion, BIM). To minimize this
43 attenuation, images are commonly recorded as a series of movie frames, each containing a

44 fraction of the total electron exposure (Brilot et al., 2012; Campbell et al., 2013; Li et al., 2013).
45 The frames are then filtered according to the radiation damage suffered by the sample, and
46 averaged into a single micrograph. We have previously developed the program *Unblur*, which is
47 part of *cisTEM* (Grant et al., 2018), to perform alignment of full movie frames and exposure
48 filtering (Grant & Grigorieff, 2015). However, as discussed in the following, full-frame
49 alignment cannot correct for local distortions and bending of the sample under the electron beam.

50 While full-frame alignment is often sufficient to achieve 3D reconstructions at near-
51 atomic resolution, more complicated patterns of sample deformation have been observed that
52 cannot be corrected in this manner. A simple model describes the deformation as a drum-like
53 motion (Brilot et al., 2012; Zheng et al., 2017; Naydenova et al., 2020), which leads to
54 differential sample motion across the field of view. The primary driver of this motion and
55 deformation is thought to be strain that develops in the sample during rapid freezing (Naydenova
56 et al., 2020; D’Imprima & Kühlbrandt, 2021).

57 Different algorithms have been developed to correct micrographs and tomograms for
58 more complicated motion patterns (Li et al., 2013; Scheres, 2014; Abrishami et al., 2015; Grant
59 & Grigorieff, 2015; Rubinstein & Brubaker, 2015; Zheng et al., 2017; Zivanov et al., 2019;
60 Tegunov & Cramer, 2019; Štrélač et al., 2020). The widely used software *MotionCor2* employs
61 polynomial equations to fit drum-like motion (Zheng et al., 2017). *Warp* (Tegunov & Cramer,
62 2019) and *CryoSPARC* (Punjani et al., 2017) use a spline-based model, which provides more
63 flexibility in representing different types of distortion. More complicated distortion models may
64 increase the resolution of 3D reconstructions of particles extracted from the corrected
65 micrographs or tomograms. However, 3D reconstruction requires multiple image processing
66 steps, and often involves additional manual decisions, making it difficult to directly measure the
67 impact of local distortion correction. Thus, it has not been quantified how great the
68 improvements by local distortion correction are, nor how different types of samples, often
69 exhibiting different degrees of distortion, benefit from it. To fill this gap, we set out to develop a
70 tool to model and visualize local motion, and to quantify the improvements in the micrographs
71 upon distortion correction.

72 In this paper, we introduce new movie alignment software, *Unbend*, along with a
73 comprehensive description of a new distortion correction model based on 3D cubic splines that is

74 designed to apply pixel-wise correction of local motion. *Unbend* features two alignment steps: a
75 full-frame alignment similar to *Unblur* (Grant & Grigorieff, 2015), which is part of *cisTEM*
76 (Grant et al., 2018), and patch-based alignment to generate reference points to initialize the 3D
77 spline model. The spline model is then refined by optimizing a summed patch-wise cross-
78 correlation loss function. The shift amount for each pixel is computed using the refined model
79 and applied to the micrograph to generate a corrected micrograph with improved high-resolution
80 signal. We also wrote *shift_field_generation*, a program that reads the refined spline parameters
81 generated by *Unbend* to plot pixel-wise shift fields for each movie frame.

82 We demonstrate the model's effectiveness using a variety of cellular sample types,
83 including whole cells (both bacterial and mammalian), lamellae (yeast and mammalian cells),
84 and cell lysates, highlighting how local motion varies across specimens. By tracking the
85 displacement of each patch from the first to the last frame, we measured the amount of motion in
86 these different samples. Using the pixel-wise shift fields of the last frame with respect to the first
87 frame, we quantified the amount of deformation and calculate the total equivalent strain (overall
88 magnitude of volumetric and deviatoric deformation, Malvern, 1969; Belytschko et al., 2000)
89 and the Von Mises equivalent strain (magnitude of deviatoric deformation, Hill, 1950). By
90 integrating these metrics with 2D template matching (2DTM) (Rickgauer et al., 2017), we
91 directly quantified the effects of local motion in the micrograph and assessed the improvement in
92 the 2DTM signal-to-noise ratio (SNR) following distortion correction. Our results show that
93 *Unbend* improves the 2DTM SNR by 3–8% and increases the number of detected targets by up
94 to 300% in a dataset, depending on the type of sample being imaged.

95 **Distortion Modeling, Correction, and Verification**

96 The alignment and local motion-correction pipeline proposed in this work consists of four
97 stages. (1) We estimate full-frame (global) shifts for each movie frame. (2) We partition the
98 globally aligned frames into patches and align each patch stack across frames to obtain per-patch
99 shift trajectories. (3) We fit these patch-wise shifts with the 3D spline deformation model
100 introduced here. (4) We refine the spline parameters by optimizing a cross-correlation-based
101 objective, and use the resulting deformation field to warp and sum frames to produce the final
102 motion-corrected micrograph (**Figure 2—figure supplement 1**). Detailed descriptions of each
103 stage and the spline model are provided below.

104 ***Full-frame alignment***

105 During the acquisition of cryo-EM data, various types of sample motion can occur,
106 including beam-induced motion and mechanical movement of the sample due to stage
107 instabilities. Correcting for this motion is an important step in obtaining high-resolution 3D
108 reconstructions of the imaged molecules. In this work, we address more complicated patterns of
109 sample motion by separately performing full-frame alignment and local distortion correction due
110 to sample deformation.

111 For full-frame alignment, we closely follow our previous version of *Unblur* (Grant &
112 Grigorieff, 2015) using alignment in three iterations with increasing resolution. The shift for
113 each frame is initially determined using the cross-correlation map between the current frame and
114 the sum of all other frames. Given the low electron exposure per frame, single-frame alignment
115 can be susceptible to noise and misalignment. A large B-factor, which can be adjusted by the
116 user, is applied during this step to suppress high-resolution noise. Sample drift due to mechanical
117 instabilities of the cryo stage is expected to be slowly varying in speed and mostly along a fixed
118 direction. This allows the full-frame shifts to be smoothed using a Savitzky-Golay (SG) filter,
119 which effectively models sample drift while preserving molecular features in the image, and
120 without introducing potential image distortions. The full-frame alignment and trajectory
121 smoothing are sufficient in many cases to achieve 3D reconstruction at near-atomic resolution
122 (Grant & Grigorieff, 2015; Oldham et al., 2016; Subramaniam et al., 2018).

123 In some cases, the shifts determined for individual frames deviates significantly from the
124 smoothed trajectory. This could be due to noise but may also reflect properties of the sample or
125 stage, and hence these outliers could represent real physical motion of the sample. Therefore,
126 solely relying on the smoothed curves means that the shifts derived from cross-correlation are
127 not directly applied in the correction, even if they represent real physical motion. To allow
128 potential discontinuities in the motion trajectories in our new approach, this smoothing function
129 is optional and is deactivated by default in *Unbend*. Instead of using the SG-filtered shifts, we
130 compare the raw shifts to the smoothed curve and identify those shifts that deviate by more than
131 1.5 times the interquartile range (IQR) from the curve. These outlier shifts are further aligned
132 using a B-factor twice that of the initial alignment (the default B-factor for the initial alignment
133 is 1500 \AA^2). If shifts remain significantly different after this adjustment, we accept them as the

134 true shifts; otherwise, we apply the new shift values. This strategy helps us detect and correct
135 potential misalignments caused by weak signal in individual frames while preserving the
136 information contained in the raw shifts about real sample motion that does not fit a smooth
137 trajectory.

138 ***Patch alignment***

139 To correct for local sample distortion, patch-based methods are widely utilized. By
140 aligning small patches across the entire micrograph, these methods can accurately capture local
141 motion. Increasing the number of patches and reducing the patch size can provide more accurate
142 local information but also limits the amount of signal per patch, leading to noisier alignments.
143 Users can set the patch size and patch numbers based on their preference. In our default settings,
144 to balance these factors, we set a patch size of 1024×1024 pixels when the output pixel size is $<$
145 0.5 \AA , and 512×512 pixels when the output pixel size is between 0.5 and 2.0 \AA . For output pixel
146 sizes $> 2.0 \text{ \AA}$, the 512×512 pixel patch size is scaled by a factor equal to the output pixel size
147 and rounded up to the nearest multiple of 16 to maintain computational efficiency.

148 The default number of patches along the x and y dimensions, denoted as NP_x and NP_y ,
149 are determined by rounding up the values of image dimensions divided by patch size. This
150 configuration minimizes overlap between neighboring patches, enabling more accurate capture
151 of local motion. Users may specify fewer patches along each dimension, resulting in larger
152 patches that capture more signal to ensure a complete coverage of the micrograph without gaps.
153 Conversely, increasing the number of patches does not reduce their size; instead, it increases the
154 percentage of overlap between adjacent patches, preserving the default patch size to ensure that
155 each patch retains sufficient signal for robust alignment.

156 Assuming that full-frame alignment has effectively removed the average motion in each
157 frame, the residual motion detected by patch alignment is primarily attributed to beam-induced
158 sample distortion. We therefore approximate the shifts determined for a given patch across
159 movie frames (a patch stack) as a smooth trajectory. For each patch stack, the alignment is firstly
160 estimated by calculating the cross-correlation between an individual frame and the average of all
161 other frames, after which the shift trajectory is smoothed using a SG filter.

162 To identify patches with unreasonable shift sets $\{(x_{pi,fi}, y_{pi,fi}) \mid fi \in \{1, 2, \dots, NF\}\}$,
163 where NF is the total number of frames, pi denotes the patch stack, and $x_{pi,fi}$ and $y_{pi,fi}$
164 represent the shift amounts along the x and y axes for frame fi in patch stack pi , we calculate
165 the standard deviation of the shift differences between neighboring frames:

$$166 \quad \sigma_{fi}(pi) = std(\Delta S_{fi}(pi)), \quad (1)$$

167 where

$$168 \quad \Delta S_{fi}(pi) = \sqrt{(x_{pi,fi+1} - x_{pi,fi})^2 + (y_{pi,fi+1} - y_{pi,fi})^2}. \quad (2)$$

169 Outliers in the set $\{\sigma_{fi}(pi) \mid pi \in \{1, 2, \dots, NP\}\}$, with $NP = NP_x \times NP_y$ as the total number of
170 patches, are detected using the $1.5 \times \text{IQR}$ upper bound criterion. Outlier shifts are then replaced
171 with the shift sets from their nearest-neighbor patches. This procedure effectively detects
172 potential misalignments caused by low signal in individual patches and provides a robust
173 initialization for the subsequent modeling of sample distortion.

174 ***Sample distortion modeling and correction***

175 Patch-wise shifts, $\{(x_{pi,fi}, y_{pi,fi}) \mid pi \in \{1, 2, \dots, NP\}, fi \in \{1, 2, \dots, NF\}\}$, represent
176 motion at the patch centers. To generate a distortion-corrected micrograph, these center shifts
177 must be interpolated to obtain the shifts of every pixel in each movie frame. This requires an
178 interpolation model, for which we employ spline functions to describe the pixel-wise shift
179 distribution across the frames.

180 **Spline model construction**

181 In this study, the spline model is constructed using uniform bicubic B-splines to describe
182 shifts in the image plane (x and y axes), and uniform cubic B-splines to constrain shifts across
183 frames (z axis/electron exposure accumulating direction). B-spline curves and surfaces comprise
184 sequences of low-degree polynomial segments, which help avoid high-degree global
185 polynomials and preserve numerical stability. For both cubic and bicubic B-splines, the model
186 guarantees C^2 continuity, i.e., it is twice continuously differentiable. This property allows for
187 smooth transitions between polynomial segments while preserving local control, since changes in
188 a control point only affect its neighboring region. As a result, the model provides sufficient
189 flexibility to capture a wide range of motion trajectories.

190 Each segment of the spline curve $S_c(t)$ is a linear combination of basic B-spline
 191 functions $B_{i,d}(t)$, weighted by neighboring control points Q_i (Farin, 2001):

$$192 \quad S_c(t) = \sum_i^{i+d} Q_i B_{i,d}(t). \quad (3)$$

193 For degree d , the blending functions $B_i^d(t)$ are defined recursively by the Cox-de Boor
 194 algorithm:

$$195 \quad B_i^0(t) = \begin{cases} 1 & t \in [t_i, t_{i+1}) \\ 0 & t \notin [t_i, t_{i+1}) \end{cases} \quad (4)$$

$$196 \quad B_i^d(t) = \frac{t-t_{i-1}}{t_{i+d-1}-t_{i-1}} B_i^{d-1}(t) + \frac{t_{i+d}-t}{t_{i+d}-t_i} B_{i+1}^{d-1}(t), \quad (5)$$

197 where $t \in [0,1]$ is a normalized parameter along the spline curve. For cubic B-splines, $d = 3$. A
 198 cubic B-spline segment can also be written in matrix formulation for better computational
 199 efficiency:

$$200 \quad S_c(t) = \frac{1}{6} [t^3 \quad t^2 \quad t^1 \quad 1] \begin{bmatrix} -1 & 3 & -3 & 1 \\ 3 & -6 & 3 & 0 \\ -3 & 0 & 3 & 0 \\ 1 & 4 & 1 & 0 \end{bmatrix} \begin{bmatrix} Q_i \\ Q_{i+1} \\ Q_{i+2} \\ Q_{i+3} \end{bmatrix}. \quad (6)$$

201 Likewise, a bicubic B-spline surface $S_s(u, v)$ follows an analogous matrix formulation:

$$202 \quad S_s(u, v) = \frac{1}{36} [v^3 \quad v^2 \quad v^1 \quad 1] M Q_{grid} \begin{bmatrix} u^3 \\ u^2 \\ u^1 \\ 1 \end{bmatrix}, \quad (7)$$

203 where M is the same 4×4 blending-function matrix, and Q_{grid} is the 4×4 arrangement of
 204 control points $\{Q_{i+k, j+l}\}$. The indices i, j specify the segment positions along the y and x axes,
 205 while $u, v \in [0,1]$ are the normalized parameters along those axes.

206 Control points and knots

207 Each cubic B-spline curve segment is defined by four control points, with each control
 208 point influencing up to four adjacent segments, whereas each bicubic B-spline surface requires
 209 sixteen control points. As shown in **Figure 1a**, control points are not located directly on the
 210 curve. The endpoints of curve segments and the four corners of the surface segments are referred
 211 to as “knots”. Adjusting the control points alters the curve’s shape, while the knots of a uniform

212 spline are evenly distributed. To determine a B-spline curve/surface, we only need to know the
213 knot parameters. The relationship between control points and knots for a curve or surface
214 segment can be expressed as (Agrapart & Batailly, 2020):

$$215 \quad K = \frac{1}{6} \Phi Q \text{ (curve)}, \quad K = \frac{1}{36} \Phi Q \text{ (surface)}, \quad (8)$$

216 where Φ is the passing matrix determined by the Cox-de Boor algorithm and the chosen
217 boundary conditions. In this work, we adopt free-end boundary conditions, allowing the spline to
218 extend linearly beyond the boundary points (**Figure 1b**). This prevents artificial curvature at the
219 edges, maintaining the natural flow of the surface without imposing strict derivative constraints.
220 For a cubic spline, the free-end boundary condition is implemented as follows:

$$221 \quad Q_{k-1} - 2Q_k + Q_{k+1} = 0, \quad k \in \{2, n + 1\}, \quad (9)$$

222 and for bicubic splines, the same condition applies along the edges. At the corners, the boundary
223 condition is:

$$224 \quad Q_{k-1,l-1} - 2Q_{k,l} + Q_{k+1,l+1} = 0, \quad k \in \{2, n + 1\}, l \in \{2, m + 1\}, \quad (10)$$

225 where m and n are the number of knots along x and y axes, respectively.

226 **Knot grid configuration**

227 Our model assigns NK_x , NK_y , and NK_z as the number of knots along the x , y , and z
228 axes, respectively. By default, NK_x and NK_y are set to two-thirds of the patch number in each
229 dimension, with a minimum of four knots, and evenly distributed along x and y . Along the z axis,
230 knots are spaced at every $4e^-/\text{\AA}^2$ of exposure, forming a three-dimensional grid together with
231 the knots along x and y . Since shifts occur in both x and y , we maintain two sets of knot
232 parameters, K_x and K_y . Given these knots, we can interpolate a dense field of shifts for every
233 pixel in each movie frame, thereby correcting local distortion in each frame.

234 **Figure 2** illustrates the knot grid and the construction of the 3D spline model. In **Figure**
235 **2a**, the spline curve for shifts along the x direction is shown along the exposure accumulation
236 direction. In this case, for a movie with 40 frames and a total exposure of $16e^-/\text{\AA}^2$, a knot is
237 assigned every 10 frames. Once the shift amounts at the knots are determined, the cubic spline
238 model, as described above, is used to compute the shift along x for each movie frame. By
239 combining these shifts with the shifts along the y -direction, we can obtain the full spline curve

240 thread as shown in **Figure 2b**. For a model with NK_x, NK_y knots along x and y , we will generate
 241 $NK_x \times NK_y$ of such 3D splines. Thus, for each movie frame, we will have a 2D grid of knots for
 242 generating the bicubic spline surface, represented by the black points in **Figure 2e**. **Figure 2c,d**
 243 show the shift fields along x and y , respectively, for a single movie frame derived using the
 244 bicubic splines. **Figure 2e** displays the image before (gray grid) and after (cyan grid) warping,
 245 based on the shift fields shown in **Figure 2c,d**. For better visualization, we amplified the
 246 distortion in these figures.

247 Parameter refinement

248 The initial refinement of knot values relies on a least-squares error minimization
 249 approach. Given the parameters K_x and K_y for the x - and y -axis, respectively, the spline model
 250 can initialize the per-patch shifts for each frame $(x_{spline}(pi, fi; K_x), y_{spline}(pi, fi; K_y))$. We
 251 estimate K_x and K_y by minimizing the following least-square loss function:

$$252 L_1(K_x, K_y) = \sum_{pi=1}^{NP} \sum_{fi=1}^{NF} ([x_{pi,fi} - x_{spline}(pi, fi; K_x)]^2 + [y_{pi,fi} - y_{spline}(pi, fi; K_y)]^2). \quad (11)$$

253 Minimizing L_1 aligns the spline model with the observed per-patch shifts, and yields the patch
 254 stack alignment result $\{(x_{pi,fi}, y_{pi,fi}) \mid pi \in \{1, 2, \dots, NP\}, fi \in \{1, 2, \dots, NF\}\}$. Because this initial
 255 fit relies solely on local per-patch information, a second round of refinement is done to
 256 incorporate global information. To this end, we define the following loss function:

$$257 L_2(K_x, K_y) = -\sum_{pi=1}^{NP} \sum_{fi=1}^{NF} CC(I_{fi}^{shifted}(pi; K_x, K_y), \bar{I}_{-fi}^{shifted}(pi; K_x, K_y)), \quad (12)$$

258 where CC denotes the cross-correlation function between a single frame in a patch stack
 259 $I_{fi}^{shifted}(pi; K_x, K_y)$ and the “leave-one-out” average of the remaining frames in the same patch
 260 stack:

$$261 \bar{I}_{-fi}^{shifted}(pi; K_x, K_y) = \frac{1}{NF-1} \sum_{\substack{fi'=1 \\ fi' \neq fi}}^{NF} I_{fi'}^{shifted}(pi; K_x, K_y). \quad (13)$$

262 Since patches with stronger signal yield larger cross-correlation values, they contribute
 263 more heavily to L_2 , thereby reducing the impact of noisier patches. The optimization algorithm
 264 L-BFGS, provided by the *dlib* package (King, 2009), is used to update parameters K_x and K_y ,
 265 producing a refined spline model that better captures the observed local movement. With these

266 optimized parameters, pixel-wise shifts are computed, and bilinear interpolation is applied to
267 calculate the densities at each output pixel, thereby generating the final motion-corrected movie
268 frames. Averaging these frames produces the final corrected micrograph. As shown in **Figure 2e**,
269 after applying the model-based shifts, areas near the edges may extend beyond or fall short of the
270 original micrograph's pixel grid. In such cases, we pad the under-extended area with the average
271 density of the edge and trim the over-extended area to fit within the boundaries of the
272 micrograph.

273 ***2DTM provides a one-step verification for motion correction***

274 2D template matching (2DTM) was originally developed to identify biomolecules in
275 images of crowded cellular environments with high precision in both location and orientation.
276 The true-positive detection is based on the 2DTM SNR at each target site (Rickgauer et al., 2017;
277 Sigworth, 2004). More specifically, at each image location p , we compute cross-correlation
278 values $CC(p, t)$ between the micrograph and the template over all sampled orientations t . We
279 then convert these values to z-scores per location $z(p, t)$, using the mean and standard deviation
280 of $\{CC(p, t)\}_t$ across orientations:

$$281 \quad z(p, t) = \frac{CC(p, t) - \mu_p}{\sigma_p}, \quad (14)$$

282 where μ_p and σ_p are the mean and standard deviation of the cross-correlation values across
283 orientations at location p . The 2DTM SNR is then defined as the maximum z-score:

$$284 \quad \text{2DTM SNR}(p) = \max_t z(p, t). \quad (15)$$

285 A detection is called when $\text{SNR}(p)$ exceeds a threshold z_{th} , which is determined based on the
286 complementary error function $r_f = \frac{1}{2} \text{erfc}\left(\frac{z_{\text{th}}}{\sqrt{2}}\right)$, where the expected false positive rate r_f is
287 calculated by assuming there is one false positive detection (1-FP criterion).

288 Because the 2DTM SNR is computed by correlating template projections with the
289 micrograph, it provides an unbiased measure of how effective the molecular signal is preserved
290 in the distortion-corrected micrograph. In the present study, we will use both the number of
291 detectable particles and their 2DTM SNR as metrics for evaluating the performance of our
292 distortion correction method.

293 We applied our model to a range of *in-situ* samples commonly studied in structural
294 biology, including whole cells (bacteria and the edges of mammalian cells), lamellae (yeast and
295 mammalian cells), and cellular lysate. Ribosomes, which can be detected with high accuracy by
296 2DTM using *cis*TEM (Grant et al., 2018), were chosen as the primary targets in the following
297 experiments. Furthermore, we also tested the performance of our new algorithm on DeCo-LACE
298 micrograph montages (Elferich et al., 2022).

299 **Results**

300 *High resolution information recovery*

301 Using the new graphical user interface (GUI) for motion correction in *cis*TEM, users can
302 readily visualize local motion by enabling the trajectory option. **Figure 3** illustrates an example
303 micrograph acquired from *Mycoplasma pneumoniae* whole-cell samples. In this case, a vortex-
304 shaped motion is observed in the region where two cells are closely adjacent to each other. This
305 type of spatially varying, non-rigid deformation would not be well captured by simple, low-order
306 global models, while the use of a continuous 3D spline representation in this work can
307 interpolate smoothly across both space and time. The patch trajectories (shown in red) are
308 magnified by a factor of 30 for clarity. **Figure 3b, c** provide zoomed-in views of the boxed area
309 and the corresponding power spectra generated from the micrograph after local distortion-
310 corrected alignment versus full-frame alignment, respectively. For movies exhibiting the highest
311 estimated motion in each sample type in this work, the recovery of Thon rings at higher spatial
312 frequencies is more apparent (see **Figure 4-figure supplements**). **Figure 3d, e** show the
313 detected particles (white projections) using 2DTM in the micrograph processed with and without
314 local distortion correction, respectively. The larger number of detected 2DTM targets
315 demonstrates that the blurring caused by the local distortion has been significantly reduced by
316 our *Unbend* program. This can also be seen in the power spectra calculated from the micrograph,
317 exhibiting more pronounced Thon rings at higher resolution after local distortion correction
318 (**Figure 3b, c**).

319 *Local motion across different samples*

320 We benchmarked our motion-correction model using three types of *in-situ* specimens:
321 whole cells, lamellae, and cell lysates. For whole cells, we used a frozen-hydrated *Mycoplasma*

322 *pneumoniae* dataset (O'Reilly et al., 2020) previously employed for the development of 2DTM
323 with *cis*TEM (Lucas et al., 2021). To enable comparison across different sample types and
324 geometries, mammalian cells were also included, specifically, immortalized *Cercopithecus*
325 *aethiops* (African green monkey) BS-C-1 kidney epithelial cells (see Materials and Methods).
326 Lamella datasets originated from two eukaryotic organisms: *Saccharomyces cerevisiae* and
327 immortalized *Mus musculus* ER-HoxB8 cells, both previously analyzed by 2DTM (Lucas et al.,
328 2022; Elferich et al., 2022). The cell lysate sample was derived from BS-C-1 cells, as described
329 in Materials and Methods.

330 To quantify the local movement, we measure the displacement of each patch's last frame
331 relative to its first frame in a micrograph $\{sh_{pi} | pi \in \{1, 2, \dots, NP\}\}$, where

$$332 \quad sh_{pi} = \sqrt{(x_{pi,NF} - x_{pi,1})^2 + (y_{pi,NF} - y_{pi,1})^2}. \quad (16)$$

333 Since the full-frame alignment is assumed to remove the global average motion, the patch
334 motions/shifts (sh_{pi}) primarily represent the BIM that reflect the sample's deformation,
335 measuring how much the patch centers are displaced from their initial positions. To characterize
336 the extent of local motion, we compute the maximum, mean, and standard deviation of these
337 shifts for each micrograph. We find that cell lysate exhibits the least local motion, whereas the
338 *Mycoplasma pneumoniae* samples demonstrate substantially larger local motions, with maximum
339 displacements of over 55 Å. *Mus musculus* cell lamella and BS-C-1 cell edge samples also show
340 considerable local motion (up to 20 Å). As indicated by the standard deviation data in **Figure 4**,
341 samples with large average patch motion also exhibit greater variability in local motion across a
342 micrograph. Such pronounced local motion will significantly attenuate high-resolution
343 information in the micrograph, making its correction essential for high-resolution cryo-EM
344 experiments.

345 To assess whether local motion correlates with specimen thickness, we estimated the
346 sample thickness using CTFFIND5 (Elferich et al., 2024) and plotted the mean shift against
347 sample thickness for each micrograph (**Figure 4b**). For consistency, all micrographs were binned
348 to 1.5 Å/pixel during alignment and outliers shown in **Figure 4a** are excluded for better pattern
349 visualization. BS-C-1 cell edge samples span a broad thickness range (50–400 nm) and their
350 mean displacements likewise cover the full range of observed shifts. *Mycoplasma pneumoniae*
351 are generally thicker (150–400 nm) and their mean displacements also distribute in the upper

352 range (2.5–6 Å). In contrast, cell-lysate specimens are thinner (50–150 nm) and exhibit the least
353 local motion, and even at the upper end (100–150 nm) of this range exhibit mean shifts below 1
354 Å. However, lamellae of similar thickness show mean displacements from < 1 Å to > 6 Å. These
355 results indicate no direct dependence of local motion on sample thickness; rather, motion
356 magnitude is highly related to the sample type and preparation method.

357 *Pixel-wise deformation quantification using equivalent strain*

358 To quantify pixel-wise shifts within each movie frame, we developed
359 `shift_field_generation`, a program that reconstructs the per-pixel displacement field of any given
360 frame by interpolating the spline parameters exported by *Unbend* during movie alignment. Using
361 the first frame as a reference, we compute the displacement of the final frame and derive two
362 complementary strain measures: Von Mises equivalent strain, which measures distortional
363 (shape-changing) effects; and total equivalent strain, which captures both volumetric (area-
364 changing) and distortional components (see Materials and Methods). Both measures range from
365 0 to infinite, with 0 designating no deformation, and provide scalar quantities that condense a
366 multi-dimensional strain (or stress) state to equivalent single-dimensional values.

367 **Figure 5** presents strain maps (per pixel) for the example micrograph shown in **Figure 3**.
368 The Von Mises (Green-Lagrange strain) map (**Figure 5a**) highlights a localized shear-dominated
369 “vortex” region where strain exceeds 1%, indicating significant non-isotropic deformation,
370 which is consistent with the rotation motion shown by the patch trajectories in **Figure 3a**. The
371 total equivalent strain map (**Figure 5b**) shows that the total equivalent strain of this area is above
372 1.4%, with the rest of the field remaining below 1.2% deformation.

373 The result in **Figure 5** is based on the alignment using a grid of 12×8 patches, which can
374 track the local strain patterns with fine granularity. Reducing the number of patches can smooth
375 small-scale fluctuations and reduce apparent peak strain values but may under-sample genuine
376 local distortions. This trade-off between patch resolution and deformation magnitude suggests
377 that the optimal patch density may depend on sample type and exposure rate. *Unbend* allows
378 users to tailor the number of patches to their specimen and exposure-fractionation scheme,
379 optimizing alignment fidelity and desired amount of deformation correction.

380 *Quantitative measurement of corrected motion using 2DTM*

381 To assess improvements in preserving high-resolution signal in the motion-corrected
382 micrographs, we searched for large ribosomal subunits (LSUs) using 2DTM, as described in the
383 Materials and Methods section. Stronger high-resolution signal leads to both an increased
384 number of detected targets (**Figure 6a**) and higher 2DTM SNR values (**Figure 6b**). We also
385 compared the SNRs of the same detections present in both micrographs processed with full-
386 frame alignment and those processed with local distortion correction. The SNR differences are
387 shown in **Figure 6c**, sorted for better visualization.

388 In whole-cell *Mycoplasma pneumoniae* samples, distortion correction resulted in a 4.2-
389 fold increase in LSU detection (95.5 vs. 22.9 detections per image), and the mean 2DTM SNR
390 improved by ~3.1% (8.96 ± 0.02 vs. 8.69 ± 0.01). The low values of standard error of the mean
391 (SEM) (0.02 and 0.01) indicate a consistent 2DTM SNR improvement. In BS-C-1 whole-cell
392 samples, the number of LSU detections increased from 55.9 to 69.1 (~23.6% improvement), and
393 the 2DTM SNR improved from 9.88 ± 0.02 to 10.42 ± 0.02 (~5.5% improvement). For targets
394 detected in both full-frame and local-distortion corrected micrographs, approximately 80%
395 showed higher 2DTM SNR values after local distortion correction (**Figure 6c**). Of the 20% of
396 detected targets that displayed lower 2DTM SNR values after local distortion correction, some
397 showed a reduction of up to a factor of 2. This reduction can be attributed to the motion
398 correction process, which optimizes an overall loss function $L_2(K_x, K_y)$ and models motion
399 using continuous functions to avoid patch alignments dominated by noise. This suggests that
400 there are local areas that happen to be well aligned using full-frame alignment, and that end up
401 with an overall worse alignment when additional degrees of freedom are added during local
402 alignment. Nevertheless, local distortion correction resulted in a 317% increase in LSU
403 detections in *Mycoplasma pneumoniae* and a 24% increase for BS-C-1, with an overall 2DTM
404 SNR improvement by 3–5%.

405 For lamellae prepared from *Saccharomyces cerevisiae* and ER-HoxB8 cells, the mean
406 number of LSU detections per micrograph increased from 350 to 401 (~15% increase) in yeast
407 samples and from 8.5 to 10.0 (~17% increase) in mammalian samples. The mean 2DTM SNR for
408 yeast sample improved from 10.18 ± 0.01 to 10.62 ± 0.01 (~4% increase), and for mammalian
409 samples, it increased from 10.4 ± 0.1 to 11.2 ± 0.1 (~8% increase). As noted earlier, motion in

410 ER-HoxB8 lamellae varies from less than 1 Å to 6 Å, contributing to a relatively larger SEM
411 value (0.1).

412 Lysates generated from BS-C-1 cells showed no substantial increase in the number of
413 LSU detections, but a 3% improvement in the 2DTM SNR was observed (from 13.84 ± 0.04 to
414 14.25 ± 0.04). As shown in **Figure 4**, cell lysates exhibit minimal local motion (mean shift
415 amount 0.7 \AA , **Figure 4-figure supplement 7**), and full-frame alignment is sufficient to correct
416 for most BIM in these samples. However, small amounts of local motion may remain and this
417 may explain the improved 2DTM SNR in 70% of the detected targets (**Figure 6c**).

418 *DeCo-LACE montages*

419 To better understand the beam-induced deformations, we analyzed a dataset of
420 micrographs collected from lamellae of *Candida albicans* cells. In this dataset, lamellae of
421 individual cells were imaged as montages (DeCo-LACE, Elferich et al., 2022). We performed
422 motion correction of the individual exposures within these montages using either full-frame
423 alignment or *Unbend*, and found that in 47 out of 82 montages, the number of detected targets
424 increased by more than 10% (**Figure 7a**). This indicates that patch-based motion correction
425 recovered signal that would otherwise have been lost to image blurring due to local deformations.
426 In some montages, the number of detected targets was substantially higher in every exposure
427 (**Figure 7c**), suggesting that these regions of the imaged lamella were generally prone to local
428 deformations and the observed increase in the number of detected targets was not due to a few,
429 heavily distorted, exposures.

430 For the remaining 35 montages that showed less than a 10% increase in target detection,
431 the number of detections remained approximately unchanged between full-frame and local-
432 distortion correction (**Figure 7b**). While we cannot rule out that areas in these lamellae
433 experienced local deformations that were not corrected by our algorithm, the overall similarity in
434 the number of detections per exposure and in the 2DTM SNR of 60S targets compared to the full
435 dataset suggests that these areas likely did not suffer from significant BIM. In fact, the mean
436 2DTM SNR in areas with less than a 10% increase in detections was 11.1, whereas the mean
437 2DTM SNR in areas with more than a 50% increase was 10.7. This suggests that patch-based
438 motion correction recovers most, but not all signal lost to local deformation.

439 In summary, our data suggest that local deformation in lamellae is not uniform: for
440 reasons that remain unclear, some lamellae remain rigid while others display local deformation.
441 Together with the finding that, despite patch-based motion correction, the average 2DTM SNR is
442 still higher in areas without deformation, we propose that future work aimed at uncovering the
443 physical basis of this variability could lead to improvements in *in-situ* cryo-EM datasets.

444 ***Comparison with published local motion correction methods using*** 445 ***2DTM***

446 Several other movie-alignment pipelines implement local motion correction using
447 different deformation models. Widely used approaches include (i) quadratic (low-order
448 polynomial) motion models, as implemented in *MotionCor2/MotionCor3* (Zheng et al., 2017),
449 and (ii) spline-based models that allow more flexible deformation fields, as implemented in
450 *Warp* (Tegunov & Cramer, 2019) and *CryoSPARC* (Punjani et al., 2017).

451 In this section, we performed movie alignment using five methods (*Unbend*, *MotionCor2*,
452 *MotionCor3*, *Warp*, and *CryoSPARC*) and then ran 2DTM on the resulting motion-corrected
453 micrographs. Because several packages only support down sampling by integer factors and all
454 movies were recorded at super-resolution, the aligned outputs were either not binned or binned
455 by a factor of two. To standardize sampling across methods and samples for downstream
456 analysis, we then Fourier-binned the corrected micrographs to a final pixel size of 1.5 Å/pixel.
457 For *Unbend*, all alignment parameters were kept at their default values. For the other packages,
458 we matched the nominal model flexibility to *Unbend*'s model by using the same number of
459 patches along x and y in *MotionCor2* and *MotionCor3*, and the same number of spline knots in
460 *Warp* and *CryoSPARC*. All remaining parameters were left at their respective defaults to
461 minimize method-specific tuning and reduce potential bias.

462 **Figure 8a** summarizes the number of 2DTM detections per micrograph for each motion-
463 correction method. For particles detected by both *Unbend* and an alternative method, we
464 computed the SNR difference as $\Delta SNR = SNR_{Unbend} - SNR_{other}$. The sorted ΔSNR
465 distributions are shown in **Figure 8b**.

466 For the *M. pneumoniae* sample, which exhibits the largest local motion (**Figure 4a**),
467 *Unbend* produced the highest detection rate, with a mean of 79.7 detections per micrograph,

468 followed by *MotionCor2* (70.6). In contrast, *CryoSPARC* produced 50.4 detections per
469 micrograph, 36.8% fewer than *Unbend*. Consistent with this, among particles detected by both
470 *Unbend* and *Warp*, over 60% had higher SNR in the *Unbend*-corrected micrographs.

471 For the cell-edge sample, where the mean patch shift spans from $<1 \text{ \AA}$ to $>5 \text{ \AA}$ (**Figure**
472 **4b**), the mean detection counts between different methods are more similar than in the bacterial
473 sample. However, the SNR comparison (**Figure 8b**) shows a clear advantage for *Unbend*: more
474 than 70% of commonly detected particles have higher SNR in *Unbend*-processed micrographs
475 than in micrographs processed by the other methods, indicating improved recovery of local
476 signal.

477 For the yeast lamella sample, performance is more consistent between methods.
478 Considering the SNR of commonly detected particles, *CryoSPARC* performs slightly better than
479 *Unbend* (only ~44% of common particles show higher SNR in *Unbend*), *MotionCor2* performs
480 similarly to *Unbend*, and *Warp* performs the slightly worse (with our choice of run parameters).
481 For the mammalian lamella sample, the methods yield similar detection counts (**Figure 8a**).
482 However, the SNR comparisons favor *Unbend*: detections from *Unbend*-processed micrographs
483 show higher 2DTM SNR than all other methods. In particular, *Unbend* yields higher SNR for
484 ~80% of the particles common with the spline-based methods (*Warp* and *CryoSPARC*). For the
485 cell-lysate sample, overlap in detections is high across methods, but 60–70% of commonly
486 detected particles still show higher SNR in the *Unbend*-corrected micrographs.

487 Overall, *Unbend* provides the best and most consistent performance across datasets in our
488 benchmark. *MotionCor2* and *MotionCor3* perform consistently and robustly across samples,
489 whereas *Warp* and *CryoSPARC* show stronger dataset dependence. We aimed to minimize user
490 bias by matching model flexibility and otherwise using default parameters; nevertheless, method-
491 specific parameter optimization could affect absolute performance. A comprehensive, method-
492 specific parameter benchmarking study is beyond the scope of this work.

493 *Unbend* runtimes

494 We benchmarked the runtimes of *Unbend* using the movie datasets analyzed in this study.
495 Each job was executed with 4 CPU threads on Intel Xeon Gold 5520+ processors. **Table 1**
496 summarizes the runtimes together with key parameters of the input movies and the
497 corresponding output micrographs. The runtimes range from ~1.5 mins to ~12.5 mins per movie,

498 depending primarily on the input image size and the number of frames. *Unbend* is currently
 499 CPU-based and therefore slower than the GPU-accelerated implementations. The most time-
 500 consuming step is the pixel-wise interpolation, which is performed on unbinned frames. This
 501 explains why larger input dimensions and higher frame numbers result in longer runtimes. A
 502 GPU-accelerated version of *Unbend*, as well as additional code-level optimizations to reduce
 503 runtime will be available in a future release.

504 **Table 1. Unbend runtimes on movies analyzed in Figure 6.**

	<i>M. pneumoniae</i>	<i>C. aethiops</i> : BS-C-1 (cell edge)	<i>S. cerevisiae</i>	<i>M. musculus</i> : ER-HoxB8	<i>C. aethiops</i> : BS-C-1 (cell lysate)
Input movie size (pixels)	5760 × 4092	5760 × 4092	11520 × 8184	11520 × 8184	11520 × 8184
No. of frames per movie	24	30	50	75	30
Exposure per frame ($e^-/\text{\AA}^2$)	1.296	1.021	0.600	0.600	1.004
No. of movies	64	65	30	59	76
Input pixel size ($\text{\AA}/\text{pixel}$)	1.053	1.33	0.53	0.415	0.415
Defocus (μm)	1.3 ± 0.5	1.5 ± 0.3	0.4 ± 0.1	1.0 ± 0.5	1.2 ± 0.4
Patch number	8 × 6	10 × 8	8 × 6	7 × 5	7 × 5
Output image size (pixels)	4044 × 2873	5107 × 3628	4070 × 2892	3187 × 2264	3187 × 2264
Output pixel size ($\text{\AA}/\text{pixel}$)	1.5	1.5	1.5	1.5	1.5
Runtime per movie (average ± standard deviation)	1m34s ± 5s	3m21s ± 35s	7m58s ± 26s	12m30s ± 43s	4m49s ± 9s

505

506 Discussion

507 In this work, we introduce *Unbend*, a cryo-EM movie alignment program that can
 508 perform local motion correction using a 3D cubic spline model. The program begins with full-
 509 frame alignment, followed by tracking of local motion via patch-based alignment. Our 3D cubic
 510 spline model is then fit to the patch motion and optimized by a summed patch-wise cross-
 511 correlation loss function, yielding refined model parameters. With this optimized model, pixel-
 512 wise shifts are calculated for each movie frame to generate the motion-corrected micrograph.
 513 *Unbend* is integrated into our *cisTEM* software, featuring a new GUI with real-time distortion
 514 visualization. Combined with our new program `shift_field_generation`, pixel-wise shift fields can

515 be generated for calculating total and Von Mises equivalent strain. These metrics quantify the
516 extent of deformation and can serve as a reference for adapting the number and overlap of
517 patches to avoid introducing excessive errors in the deformation model.

518 ***Model performance***

519 We validated *Unbend* across diverse *in-situ* samples, including whole cells, lamellae, and
520 cell lysates, and used 2DTM to quantify the improvement in high-resolution signal in the
521 motion-corrected micrographs. Across all sample types tested, *Unbend* boosted 2DTM SNR by 3
522 –8% and the number of detected targets by up to 300%, with the largest gains observed in
523 specimens exhibiting large local motion (whole cells and lamellae). While cell lysate showed
524 minimal local motions, a 3% improvement in 2DTM SNR was still observed.

525 Equivalent-strain analysis confirmed that, apart from some samples of the *M.*
526 *pneumoniae* dataset, correction-induced deformations remain below 1.0%, suggesting that the
527 model improves alignment without introducing excessive errors. The strain fields showing the
528 maximum patch shift amounts in micrographs of different samples in **Figure 4** are presented in
529 **Figure 4—figure supplement 1–5** and summarized in **Figure 4—figure supplement 6**. For the
530 *M. pneumoniae* sample in **Figure 4—figure supplement 1**, strain analysis revealed maximum
531 Von Mises and total equivalent values exceeding 2.2% and 3.5%, respectively, consistent with
532 plastic deformation. Comparison of the corresponding power spectra (**Figure 4—figure**
533 **supplement 1a,b**) showed that the micrographs corrected with *Unbend* displayed stronger Thon
534 rings at high spatial frequencies, confirming that the observed plastic deformation was, at least
535 partially, accommodated.

536 Together, these results demonstrate that local motion correction is essential for obtaining
537 fully motion-corrected micrographs, especially when imaging whole cells and lamellae.

538 ***Implications and limitations***

539 Our results indicate that specimen type and preparation method strongly influence local
540 sample motion. Whole cells often exhibit large thickness gradients that can potentially create
541 areas of differential motion under the electron beam, while in lamellae, which are generally
542 thinner and more homogeneous, some stress may still be present due to the milling process and
543 residual sample inhomogeneity. The local distortion correction model is particularly beneficial in

544 this context, as it can compensate for these localized motion artifacts, leading to more accurate
545 particle detection and improved 2DTM SNR. Cell lysates typically show less localized motion,
546 and full-frame alignment is sufficient for detecting most targets using 2DTM, although some
547 residual local distortion remains detectable and correctable.

548 Lamellae montages collected using DeCo-LACE (Elferich et al., 2022) further revealed
549 substantial spatial heterogeneity in the amount of local motion, indicated by the range of 2DTM
550 detection gains from under 10% to over 50% within a single sample. We found that montages
551 with less motion better preserve high-resolution signal, suggesting that further improvements in
552 the motion correction model, perhaps based on a more detailed physical mechanism, may yield
553 additional benefits. For single particle samples, which are generally thin and homogeneous, local
554 motion is less pronounced, and full-frame alignment should be sufficient in most cases.
555 Therefore, they were not tested in this work.

556 **Materials and methods**

557 **Key resources table.**

Reagent type (species) or resources	Designation	Source or reference	Identifier	Additional information
Cell line (<i>Mycoplasma pneumonia</i>)	M129	O'Reilly et al., 2020; Lucas et al., 2021		
Cell line (<i>Cercopithecus aethiops</i>)	BS-C-1	ATCC	CCL-26	
Cell line (<i>Mus musculus</i>)	ER-HoxB8	Elferich et al., 2022		
Cell line (<i>Saccharomyces cerevisiae</i>)	BY4741	Lucas et al., 2022		
Cell line (<i>Candida albicans</i>)		Elferich et al., 2025		
Software, algorithm	cisTEM	Lucas et al., 2021; Grant et al., 2018; Elferich et al., 2024		https://cistem.org/

558 559 ***Cell culture, cell lysate and grid preparation***

560 Adherent BS-C-1 cells were cultured as previously described by (Salgado et al., 2018).
561 Briefly, cells were maintained at 37°C in a humidified atmosphere with 5% CO₂ and grown in
562 Dulbecco's Modified Eagle Medium (DMEM; Invitrogen) supplemented with 10% fetal bovine
563 serum (FBS), 1X GlutaMAX (Thermo Fisher Scientific), and 1% penicillin-streptomycin (100

564 U/mL penicillin and 100 µg/mL streptomycin; Thermo Fisher Scientific). For grid seeding, cells
565 were washed twice with pre-warmed PBS and detached using trypsin-EDTA (Gibco). Cells were
566 counted, diluted to 1×10^5 cell/ml and seeded onto fibronectin-coated (5 µg/mL in PBS) EM
567 grids.

568 Double-side glow-discharged, 200-mesh gold grids with a silicon oxide support film
569 containing 2 µm holes and 2 µm spacing (Quantifoil) were used. Prior to use, grids were cleaned
570 by three washes with ethyl acetate and exposed to UV light under a laminar flow hood for 45
571 minutes. Grids were placed into 35 mm glass-bottom tissue culture dishes (MatTek) for cell
572 growth. Cells were allowed to adhere and spread for 24–48 hours before vitrification. Each grid
573 was inspected under an inverted light microscope to confirm appropriate cell density and carbon
574 film integrity. We aimed for approximately one cell per mesh; grids with excessive cell clumping
575 were excluded.

576 Immediately before plunge freezing, grids were washed twice with warm PBS and
577 transferred into Minimum Essential Medium Eagle Alpha (MEM α ; Sigma) supplemented with
578 25 mM of HEPES buffer. Grids were then rapidly moved from the incubator to a Leica GP2
579 cryo-plunger, excess liquid was blotted from the back side for 8 seconds, and grids were plunge-
580 frozen into liquid ethane cooled to -184 °C.

581 Cell extracts were prepared from BSC-1 cells using digitonin-based semi-
582 permeabilization. Briefly, cells were seeded in a 75 cm² flask and cultured to confluence. After
583 washing twice with pre-warmed PBS, the cells were detached with Trypsin-EDTA (Gibco) and
584 collected by centrifugation at $300 \times g$ for 4 minutes. The cell pellet was resuspended in 100 µL
585 of semi-permeabilization buffer (25 mM HEPES, 110 mM potassium acetate, 15 mM
586 magnesium acetate, 1 mM DTT, 0.015% digitonin, protease inhibitor cocktail (1 tablet/ 10 ml;
587 Roche), 40 U/mL RNase In (Promega), 1 mM EGTA) and 4 °C for 5 minutes. Following
588 centrifugation at $1,000 \times g$ for 5 minutes, the supernatant was collected for use in grid
589 preparation without further modification. RNA concentration was quantified prior to grid
590 preparation as a quality control measure, with no dilution of the extract performed. Glow-
591 discharged Quantifoil 200-mesh gold grids with a silicon oxide support film containing 2 µm
592 holes and 2 µm spacing were used. Plunge freezing conditions used were identical to those
593 described for whole cells.

594 ***Cryo-EM data acquisition***

595 Cryo-EM data were collected using a Titan Krios transmission electron microscope
596 (Thermo Fisher Scientific) operated at 300 keV, equipped with a K3 direct electron detector and
597 an energy filter (Gatan) set to a 20 eV slit width.

598 For cell edge data collection, medium magnification montages were used to select
599 vitrified cell areas that were transparent enough for cryo-EM. Images were acquired at a nominal
600 magnification of 64,000 \times corresponding to a calibrated pixel size of 1.33 Å. A defocus range of
601 -1.0 to -1.5 μm was targeted using SerialEM's autofocus function (Mastronarde, 2005) on a
602 sacrificial area. Movies were recorded at an exposure rate of $1.02 e^-/\text{\AA}$ per frame to a total
603 accumulated exposure of $30.6 e^-/\text{\AA}$.

604 For the cell lysate, we used a nominal magnification of 105,000 \times corresponding to a
605 calibrated pixel size of 0.83 Å. We employed beam tilt to acquire multiple movies (5 per hole
606 across nine holes) at each stage position. Zero-loss peak (ZLP) refinement was performed every
607 90 minutes at a unique location to avoid dark areas. Movies containing 30 frames, with an
608 exposure of $1.0 e^-/\text{\AA}$ per frame, were recorded, resulting in a total exposure of $30 e^-/\text{\AA}$.

609 ***2D template generation and 2D template matching***

610 For 2DTM, 3D templates were generated from trimmed atomic models containing only
611 the large ribosomal subunit (50S or 60S), using the simulate program (Himes & Grigorieff,
612 2021). Specifically, models derived from PDB entries 5LZV (for mammalian samples: BS-C-1
613 and ER-HoxB8), 6Q8Y (for *Saccharomyces cerevisiae*), and 3J9W (for *Mycoplasma*
614 *pneumoniae*) were used. The defocus of the micrographs was determined using CTFFIND5.
615 2DTM was performed using the match_template program (Lucas et al., 2021) as implemented in
616 cisTEM. The search was conducted with an in-plane angular step of 1.5° and an out-of-plane
617 step of 2.5° . For whole-cell and lamella samples, an additional defocus search was conducted
618 within ± 120 nm of the estimated defocus, using 20 nm increments.

619 Template-matched coordinates, Euler angles, and defocus values were extracted using the
620 MT module within the cisTEM GUI and exported as .star files. These files were subsequently
621 analyzed to quantify the number of detected targets and the 2DTM SNR using custom Python

622 package (https://github.com/LingliKong/2DTMSNR_MoCo_Bench). The sample thickness was
623 determined using CTFFIND5.

624 *Von Mises equivalent strain and total equivalent strain*

625 The Von Mises equivalent strain derives from the Von Mises criterion, widely used in
626 engineering and mechanics to predict yielding or failure of materials subjected to complex
627 (multiaxial) stresses or strains. The Von Mises equivalent strain effectively measures how far a
628 material is distorted from its original shape. In our case, with the shift field $\{u_x, u_y\}$, we can
629 obtain the deformation gradient \mathbf{F} :

$$630 \quad \mathbf{F} = \mathbf{I} + \nabla \mathbf{u} = \begin{pmatrix} 1 + \frac{\partial u_x}{\partial x} & \frac{\partial u_x}{\partial y} \\ \frac{\partial u_y}{\partial x} & 1 + \frac{\partial u_y}{\partial y} \end{pmatrix}. \quad (17)$$

631 The Green-Lagrange strain tensor \mathbf{E} filters out the rigid-body rotations measures the true finite
632 strains, and can be calculated by:

$$633 \quad \mathbf{E} = \frac{1}{2}(\mathbf{F}^T \mathbf{F} - \mathbf{I}) = \begin{bmatrix} E_{xx} & E_{xy} \\ E_{xy} & E_{yy} \end{bmatrix}. \quad (18)$$

634 The total equivalent strain combines the magnitude of all deformation modes (axial + shear) and
635 is expressed as:

$$636 \quad \varepsilon_{total_eq} = \sqrt{\mathbf{E}_{ij} \mathbf{E}_{ij}} = \sqrt{E_{xx}^2 + E_{yy}^2 + 2E_{xy}^2}. \quad (19)$$

637 The Von Mises equivalent strain removes the volume change and only keep the shape change:

$$638 \quad \varepsilon_{vm_eq} = \sqrt{\frac{2}{3} E_{ij}^{dev} E_{ij}^{dev}} = \sqrt{\frac{2}{3} \left[\left(E_{xx} - \frac{E_{xx} + E_{yy}}{3} \right)^2 + \left(E_{yy} - \frac{E_{xx} + E_{yy}}{3} \right)^2 + 2E_{xy}^2 \right]}, \quad (20)$$

639 where E_{ij}^{dev} is the deviatoric strain:

$$640 \quad E_{ij}^{dev} = E_{ij} - \frac{1}{3} (tr \mathbf{E}) \delta_{ij}. \quad (21)$$

641 δ_{ij} is the Kronecker delta, and $tr \mathbf{E}$ is the volumetric part/trace, which represent the pure
642 “dilation” or “compression” component that changes the area but not shape:

$$643 \quad tr \mathbf{E} = E_{xx} + E_{yy}. \quad (22)$$

644 **Data availability**

645 Movies of samples not published previously have been deposited on EMPIAR: movies of
646 ER-HOXB8 cells (EMPIAR-12944); movies of BS-C-1 cell edges (EMPIAR-12943); movies of
647 BS-C-1 cell lysate (EMPIAR-12942). The source code for *Unbend* is part of *cisTEM* and
648 available at <https://github.com/timothygrant80/cisTEM/tree/unbend>; binaries for most Linux
649 distributions can be downloaded at <https://cistem.org/downloads>. The 2DTM detection and SNR
650 comparison script is available at https://github.com/LingliKong/2DTMSNR_MoCo_Bench.

651

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657

658 **Author contributions**

659 Conceptualization: L.K., J.E. and N.G.; Data curation: L.K., X.Z. and J.E.; Formal
660 analysis: L.K., X.Z. and J.E.; Funding acquisition: N.G.; Investigation: L.K., X.Z. and J.E.;
661 Methodology: L.K., J.E., and N.G.; Project administration: L.K. and N.G.; Resources: L.K., X.Z.,
662 J.E., and N.G.; Software: L.K., J.E. and N.G.; Supervision: N.G.; Validation: L.K., X.Z., J.E. and
663 N.G.; Visualization: L.K., X.Z., J.E. and N.G.; Writing – original draft: L.K., X.Z., J.E. and N.G.;
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665

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758

760 **Figure legends**

761 **Figure 1** Uniform cubic spline curve **(a)** Diagram showing the core components of a cubic B-
762 spline curve, such as knots, control points, and the uniform knot positions t_i . **(b)** Diagram
763 showing the free-end boundary condition for a cubic B-spline.

764 **Figure 2** 3D spline model knot grid construction and shift field generation. **(a)** Diagram showing
765 the position of knots along the exposure accumulation direction and the shift amount along x for
766 each movie frame. **(b)** A 3D diagram showing the cubic B-spline along the exposure
767 accumulation direction, with red arrows representing the shifts where the knots are located (black
768 dots on the gray line), and the cyan curve showing the spline curve for interpolating the shifts for
769 each frame. **(c, d)** Shift field along x and y showing the shift amount of each pixel obtained from
770 the bicubic B-splines on a 30×30 pixels frame (for demonstration only). **(e)** Schematic image
771 grid before (gray grids) and after (cyan grid) applying the shift fields in **(c, d)**. The red arrows
772 represent the shift of patches. Black dots represent knot positions.

773 **Figure 3** A micrograph of whole-cell *Mycoplasma pneumoniae*. **(a)** Motion trajectory panel in
774 the *cis*TEM GUI. **(b)** The cropped area shown in (a) without local distortion correction,
775 experiencing blurring due to the local distortion (upper) and the power spectrum (lower). **(c)** The
776 cropped area (upper) and the power spectrum of the local distortion-corrected micrograph
777 (lower). **(d)** Detected particles (white) using 2DTM on the full-frame aligned micrograph. **(e)**
778 Detected particles (white) using 2DTM on the local-distortion corrected micrograph.

779 **Figure 4** Patch shift in different types of samples. **(a)** Box plots of the standard deviation of
780 patch motions calculated for micrographs of different types of samples. **(b)** The mean patch
781 shifts for each micrograph, colored by sample type.

782 **Figure 5** Magnitude of deformation correction of the micrograph shown in **Figure 3a**. (a) Von
783 Mises equivalent strain and (b) total equivalent strain.

784 **Figure 6** Evaluation of local motion correction using *Unbend* across different sample types. **(a)**
785 Box plots displaying the distribution of the number of 2DTM detections per micrograph. **(b)**
786 Histograms of the 2DTM SNR of detected 2DTM targets. *Unbend* improves the overall
787 distribution of SNR values for all sample types. **(c)** 2DTM SNR difference between *Unbend* and

788 *Unblur*. Across all sample types, *Unbend* led to improvements in either the number of detected
789 targets or 2DTM SNR values, or both.

790 **Figure 7** Impact of patch-based motion correction on detection of 60S subunits in focused ion
791 beam-milled lamellae analyzed in a large dataset. **(a)** Histogram showing the percentage of
792 increase of 60S detection in montages processed using *Unbend*, compared to *Unblur*. **(b)**
793 Scatterplot of the number of detected 60S per exposure in a representative montage that did not
794 show a substantial increase of detection after processing with *Unbend*, compared to *Unblur*. **(c)**
795 Similar to panel **(b)**, but for a representative montage with a more substantial increase of
796 detected targets after processing with *Unbend*, compared to *Unblur*.

797 **Figure 8** Comparison of local motion-correction methods. (a) Box plots showing the distribution
798 of the number of 2DTM detections per micrograph for each motion correction method. (b)
799 Distribution of 2DTM SNR differences between *Unbend* and the other tested methods for
800 particles detected in common ($\Delta SNR = SNR_{Unbend} - SNR_{other}$). Vertical lines mark the zero-
801 crossing in the sorted ΔSNR distribution for each method. Percentages in the legend indicate the
802 fraction of commonly detected particles with higher SNR in *Unbend*-processed micrographs.

803 **Figure 2—figure supplement 1** *Unbend* movie alignment and local motion correction algorithm.

804 **Figure 4—figure supplement 1** *Mycoplasma pneumoniae* sample. (a) Screen shot of the
805 *cis*TEM GUI displaying the motion-corrected micrograph and patch trajectories. (b) Micrograph
806 based on full-frame alignment. (c) Von Mises equivalent strain field. (d) Total equivalent strain
807 field.

808 **Figure 4—figure supplement 2** BS-C-1 cell edge sample. (a) Screen shot of the *cis*TEM GUI
809 displaying the motion-corrected micrograph and patch trajectories. (b) Micrograph based on full-
810 frame alignment. (c) Von Mises equivalent strain field. (d) Total equivalent strain field.

811 **Figure 4—figure supplement 3** *Mus musculus* ER-Hoxb8 cell lamella sample. (a) Screen shot
812 of the *cis*TEM GUI displaying the motion-corrected micrograph and patch trajectories. (b)
813 Micrograph based on full-frame alignment. (c) Von Mises equivalent strain field. (d) Total
814 equivalent strain field.

815 **Figure 4—figure supplement 4** *Saccharomyces cerevisiae* lamella sample. (a) Screen shot of
816 the *cis*TEM GUI displaying the motion-corrected micrograph and patch trajectories. (b)
817 Micrograph based on full-frame alignment. (c) Von Mises equivalent strain field. (d) Total
818 equivalent strain field.

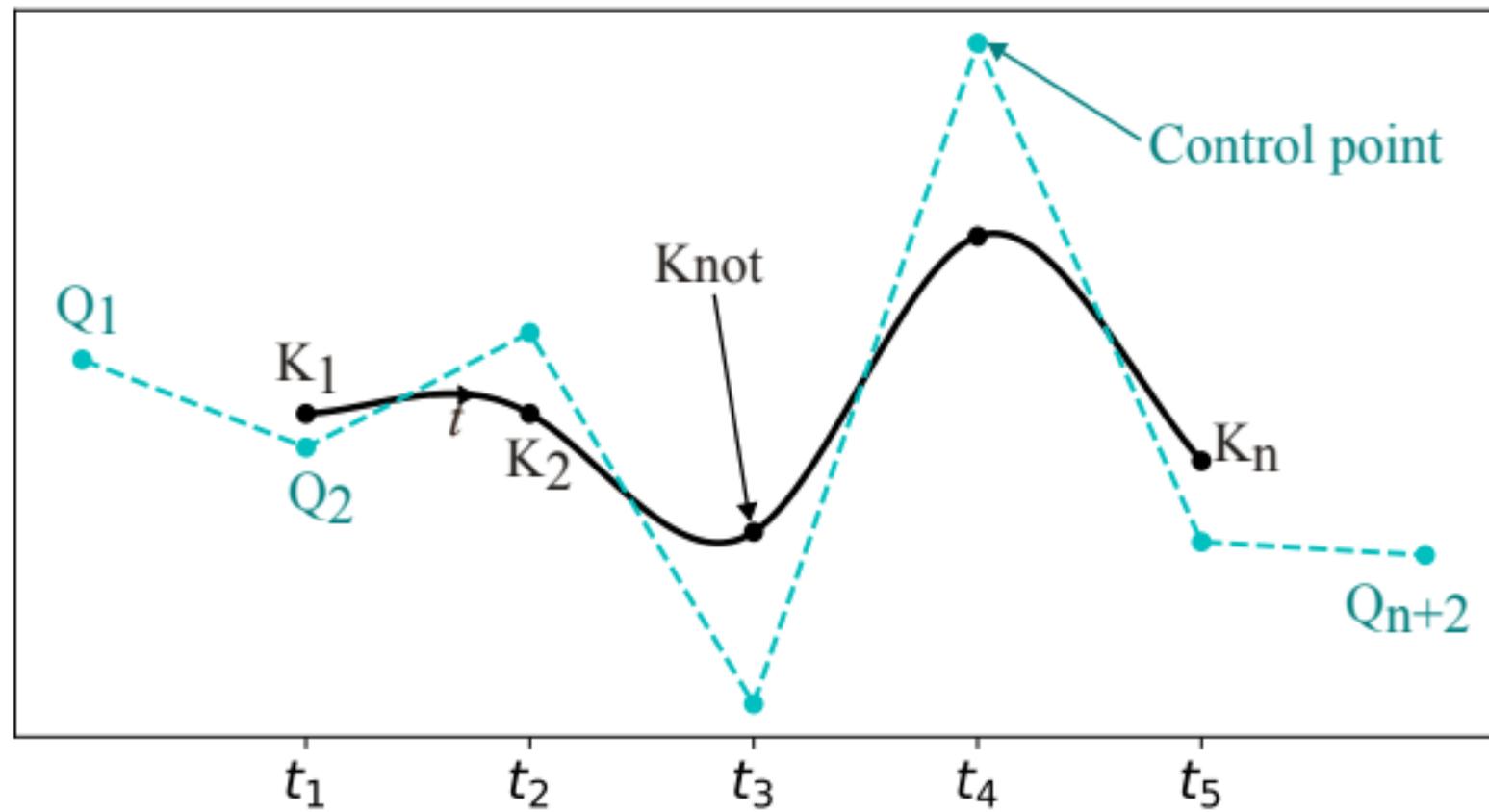
819 **Figure 4—figure supplement 5** BS-C-1 cell lysate sample. (a) Screen shot of the *cis*TEM GUI
820 displaying the motion-corrected micrograph and patch trajectories. (b) Micrograph based on full-
821 frame alignment. (c) Von Mises equivalent strain field. (d) Total equivalent strain field.

822 **Figure 4—figure supplement 6** Motion and equivalent strain summary table for micrographs
823 shown in **Figure 4—figure supplements 1–5**.

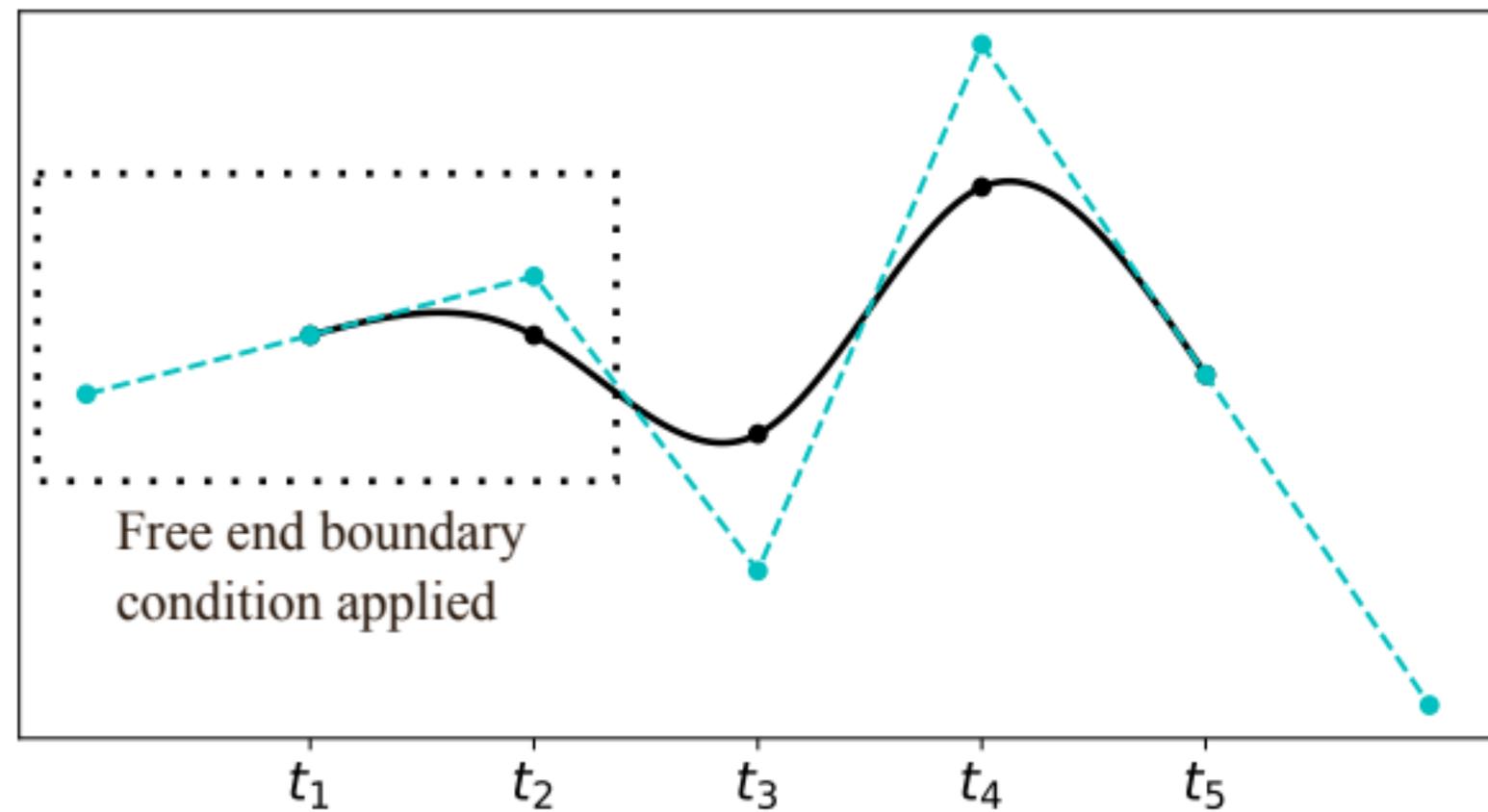
824 **Figure 4—figure supplement 7** Summary statistics of per-micrograph mean patch shifts by
825 sample type.

826 **Figure 8—figure supplement 1** Statistics table for detected particles from micrographs
827 processed by different software.

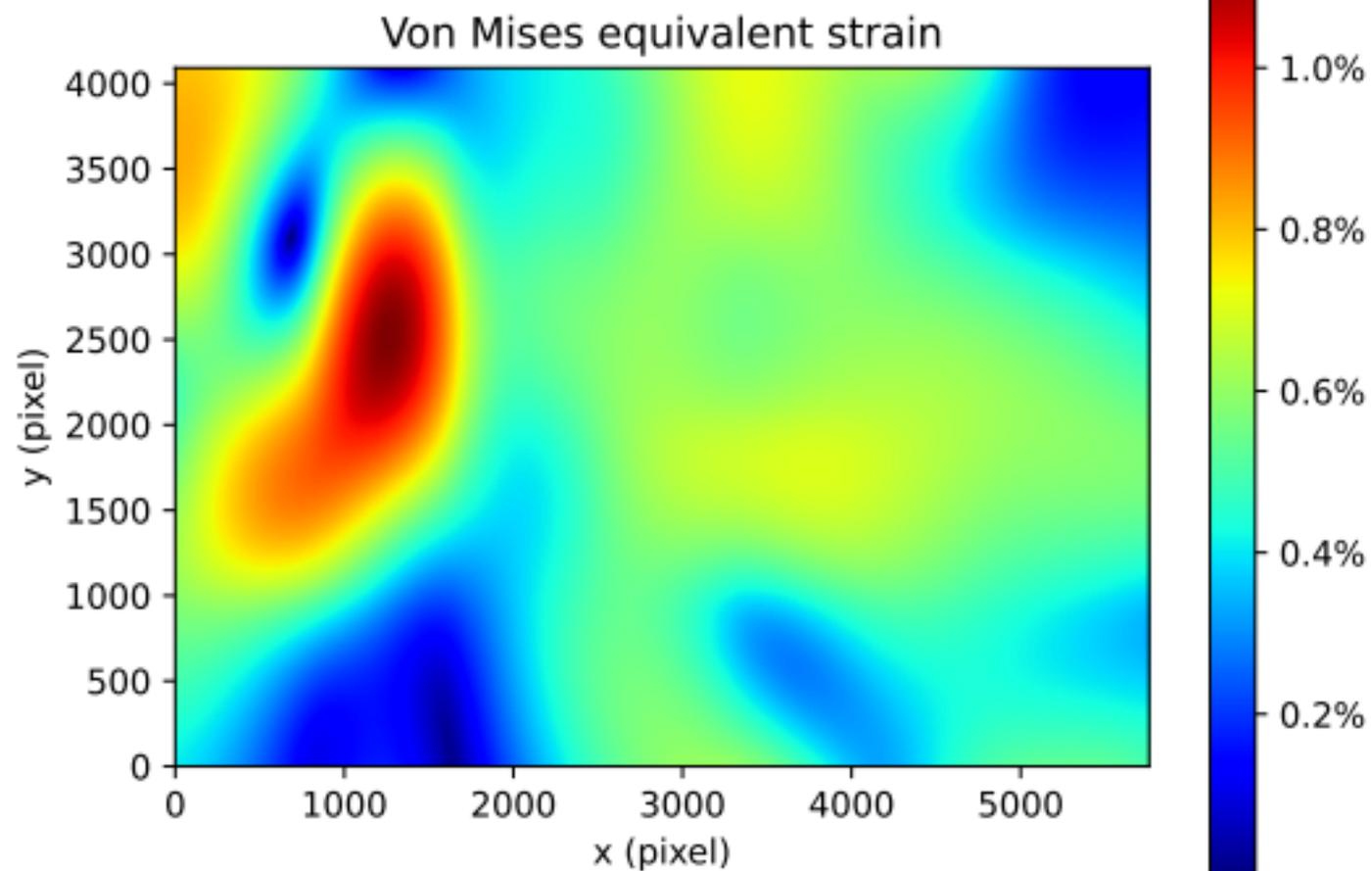
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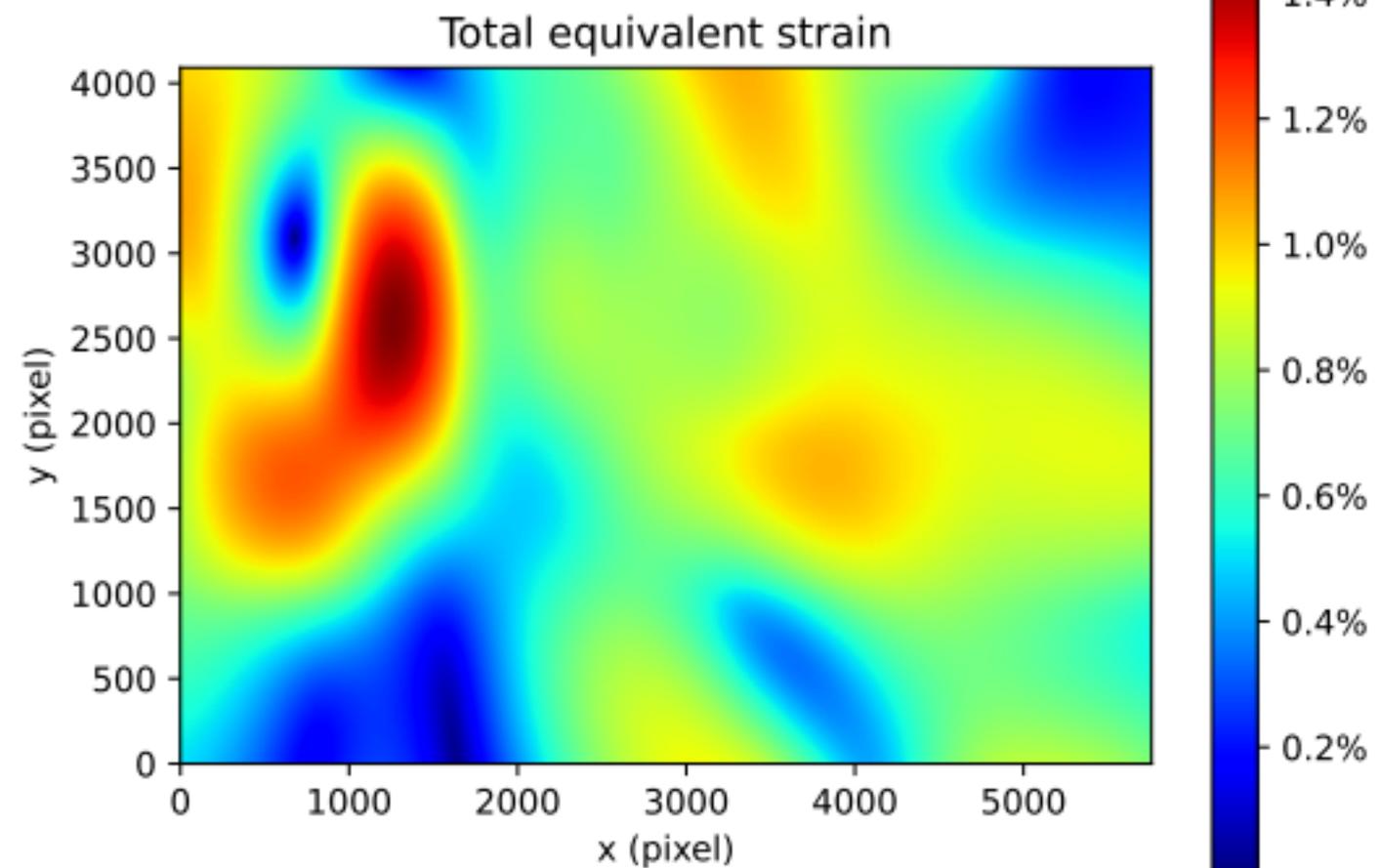
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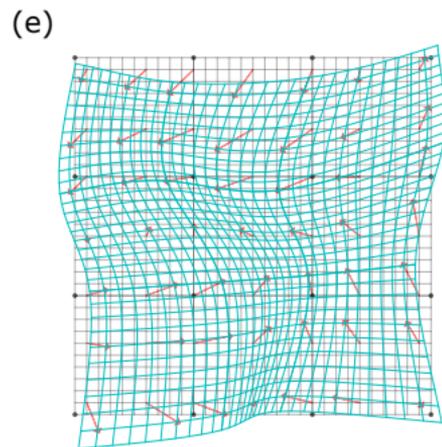
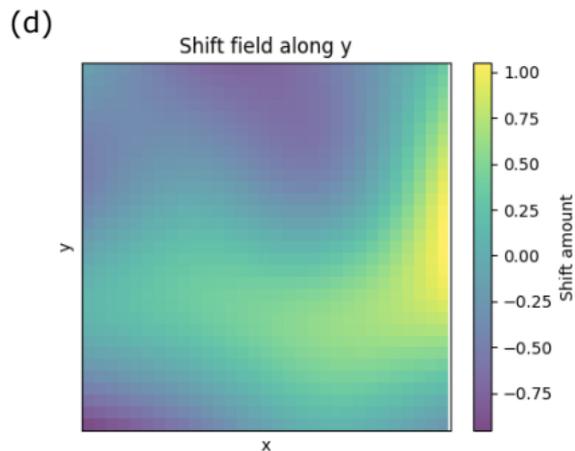
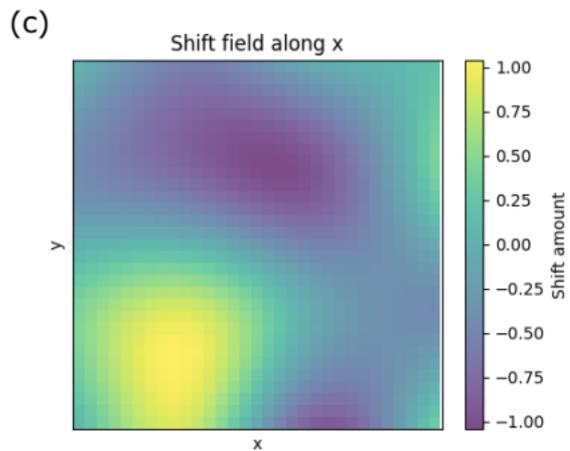
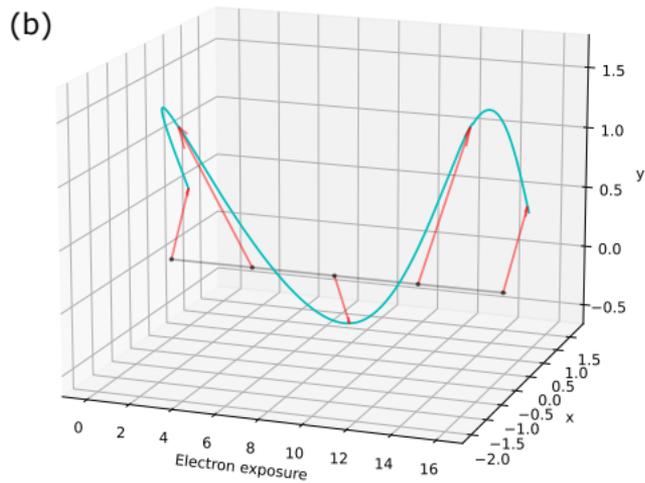
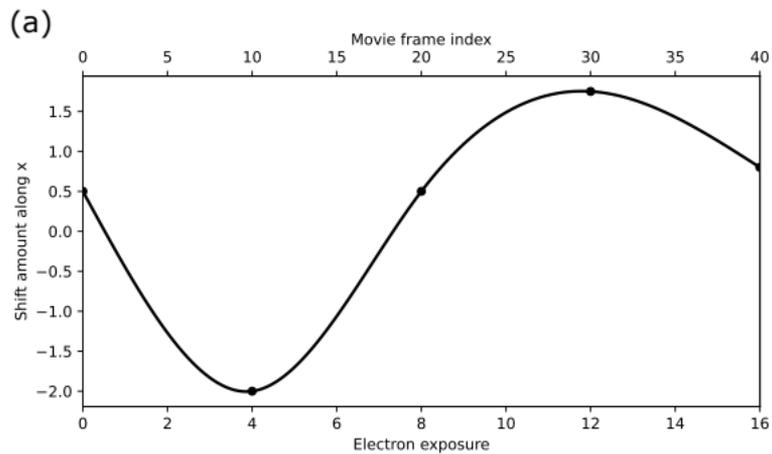


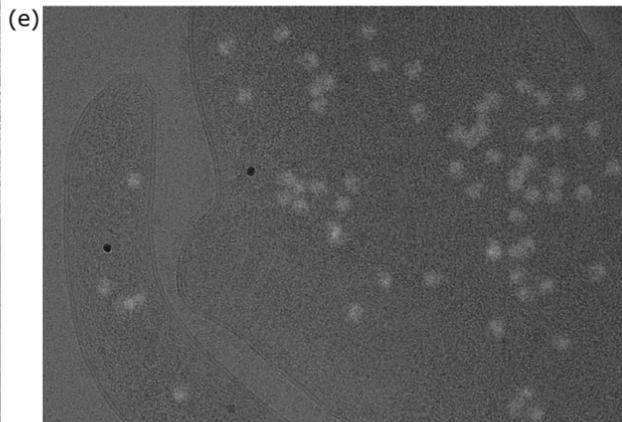
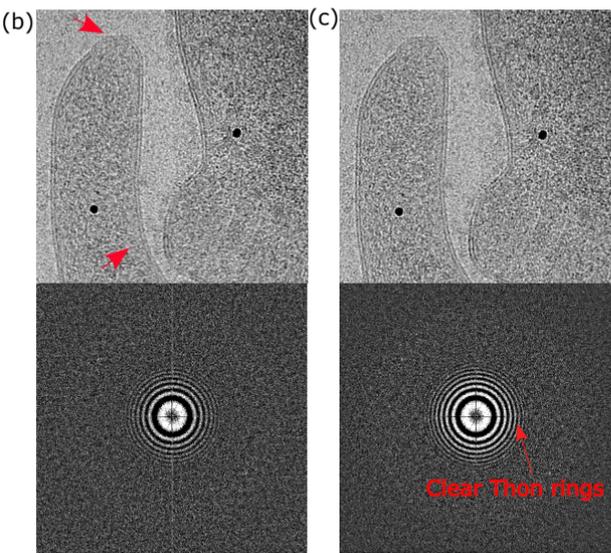
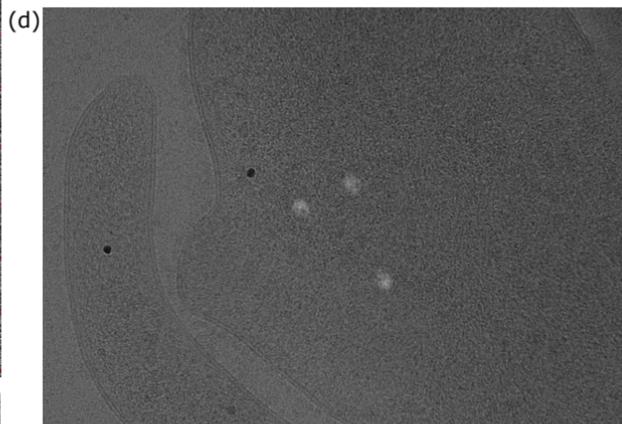
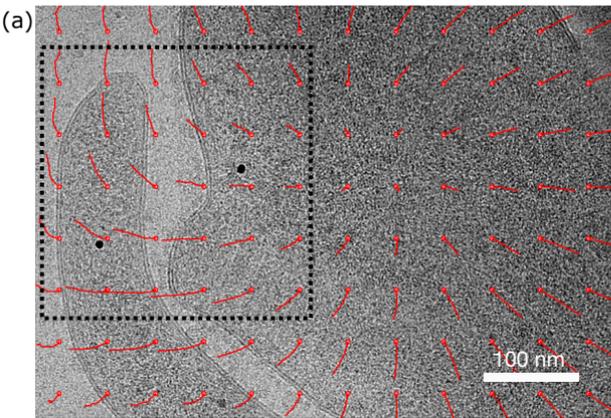
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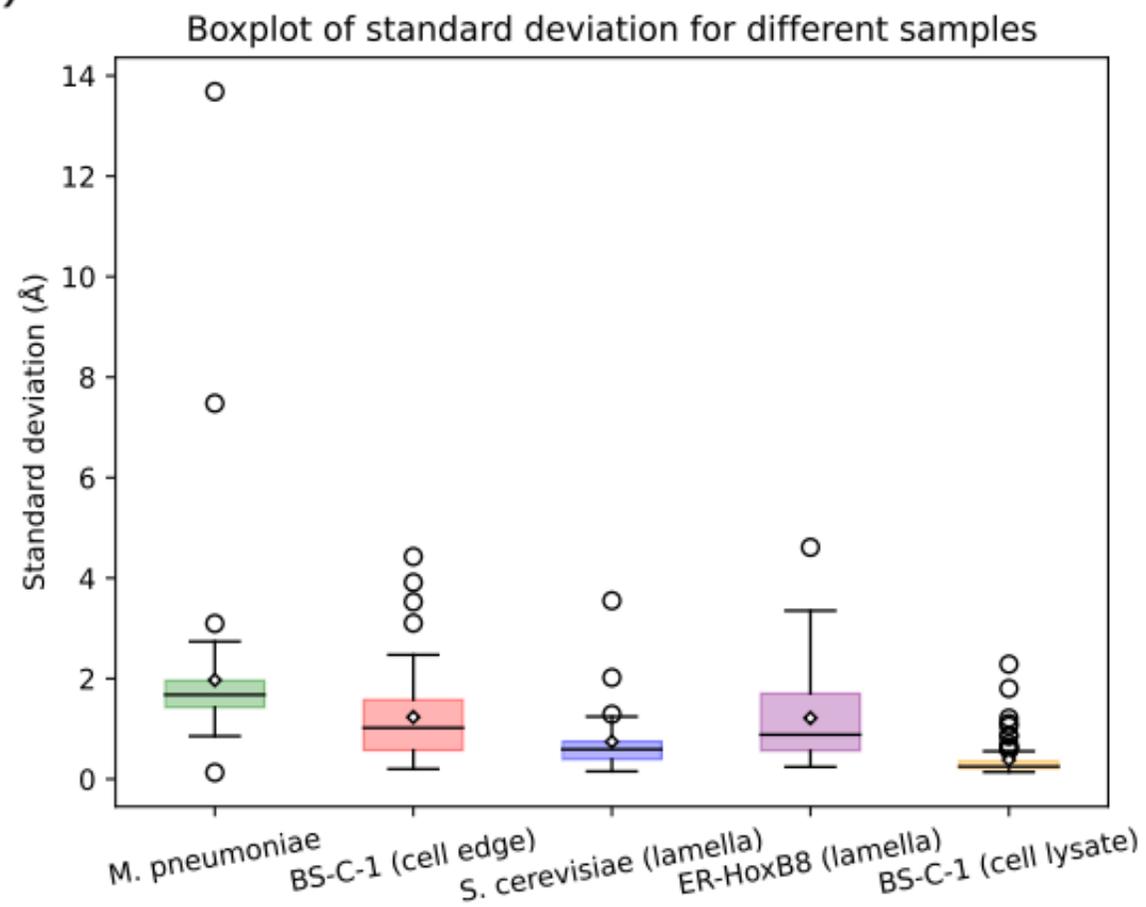
(b)







(a)



(b)

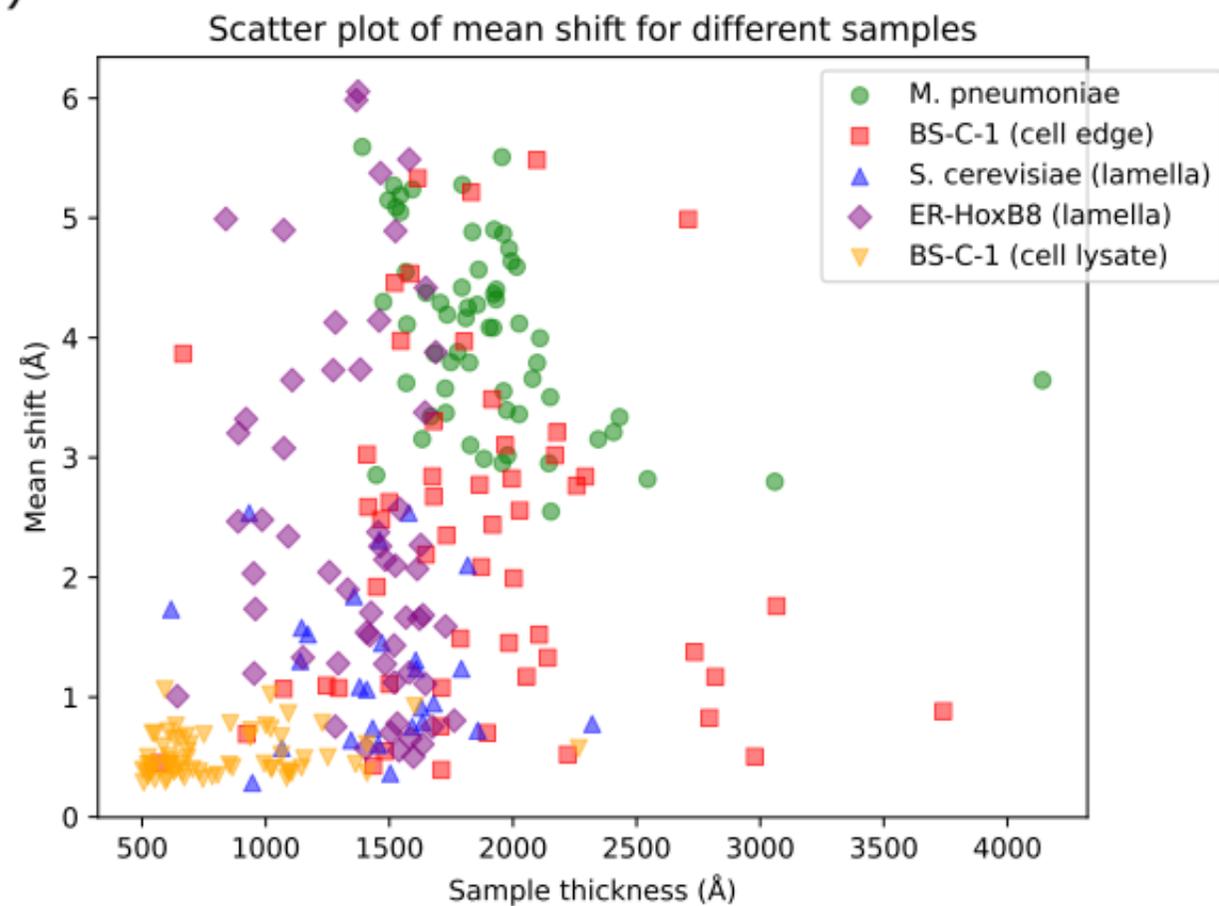
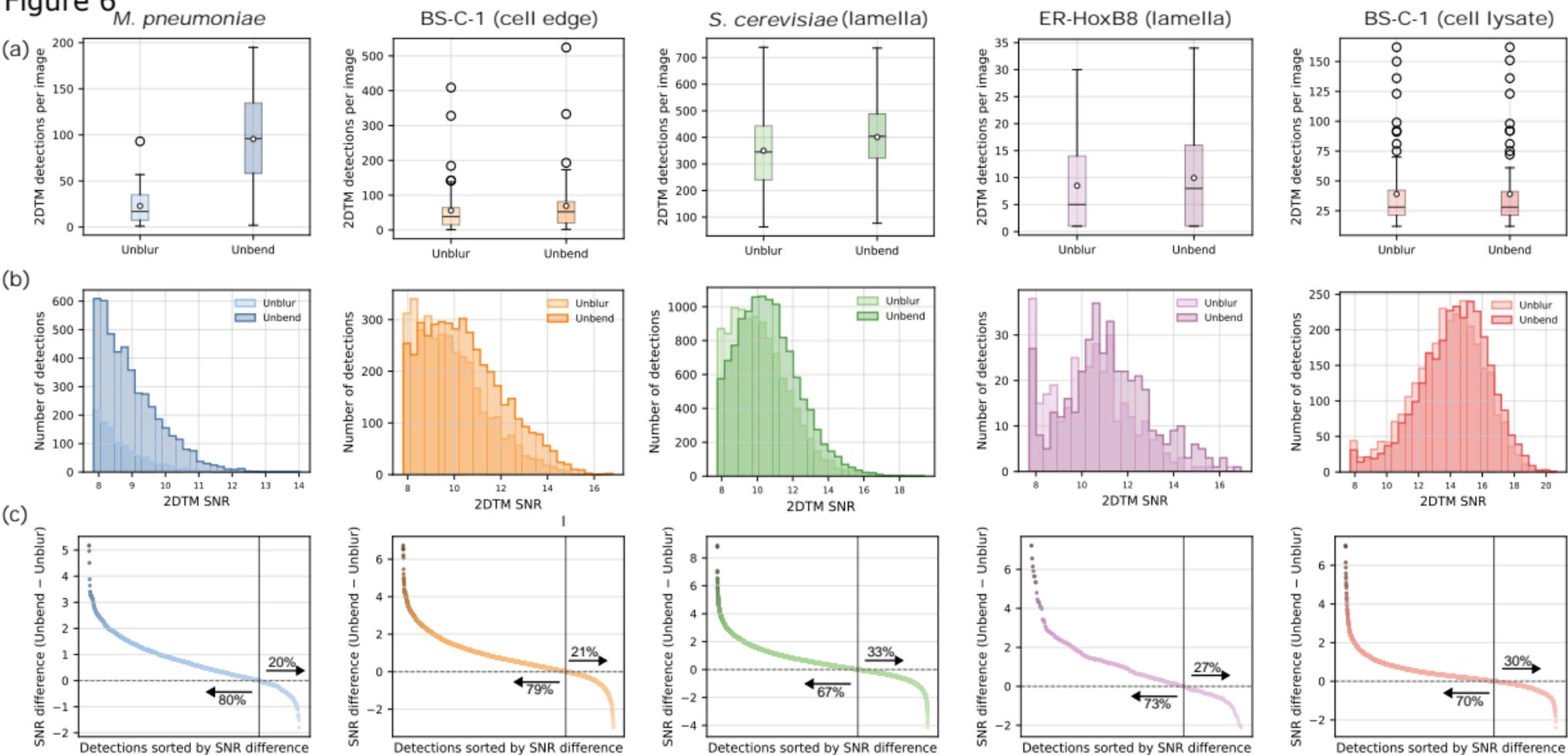
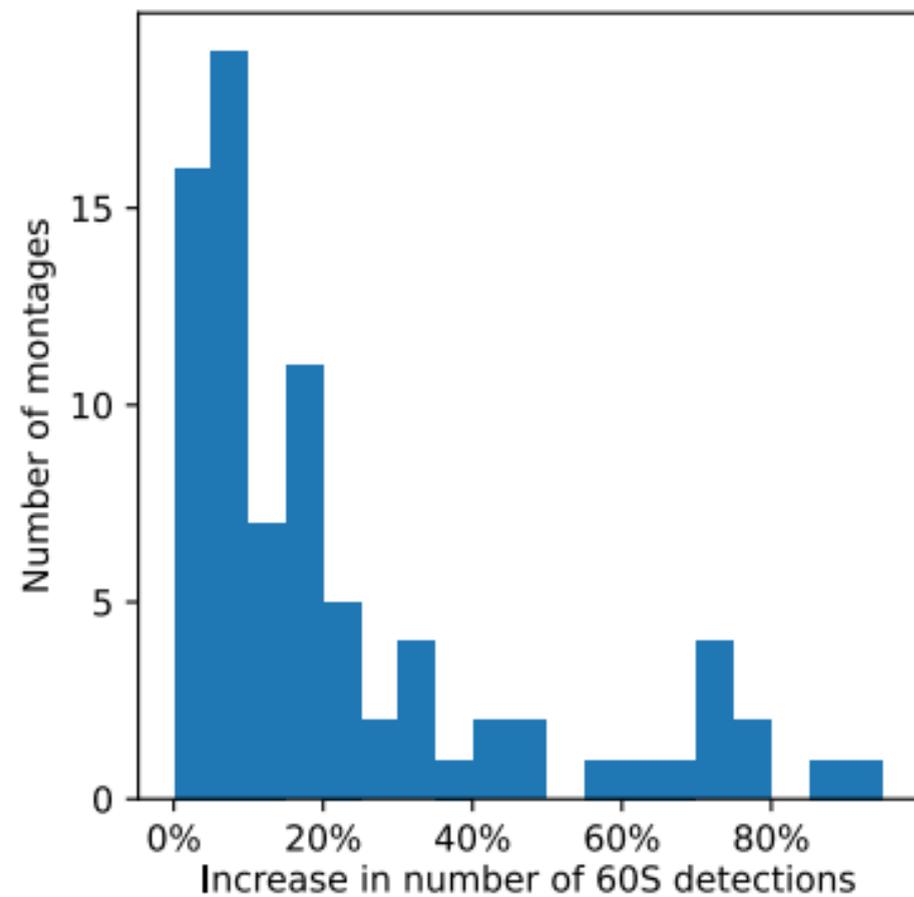


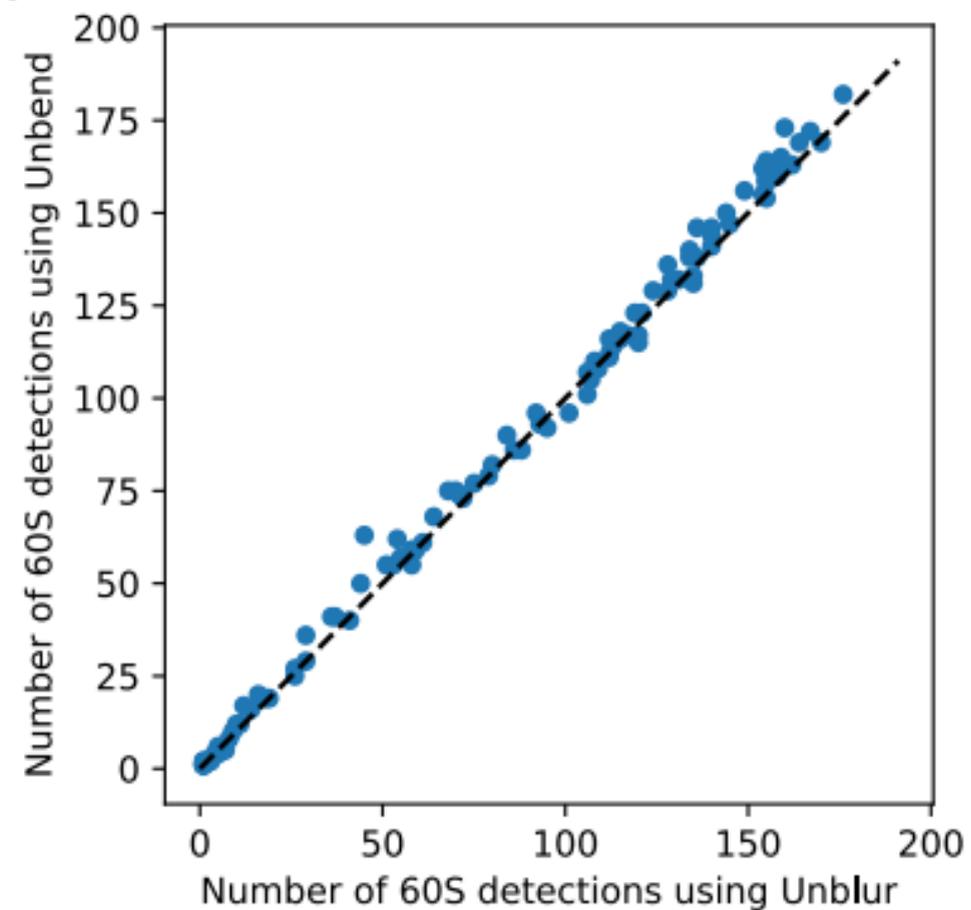
Figure 6 *M. pneumoniae*



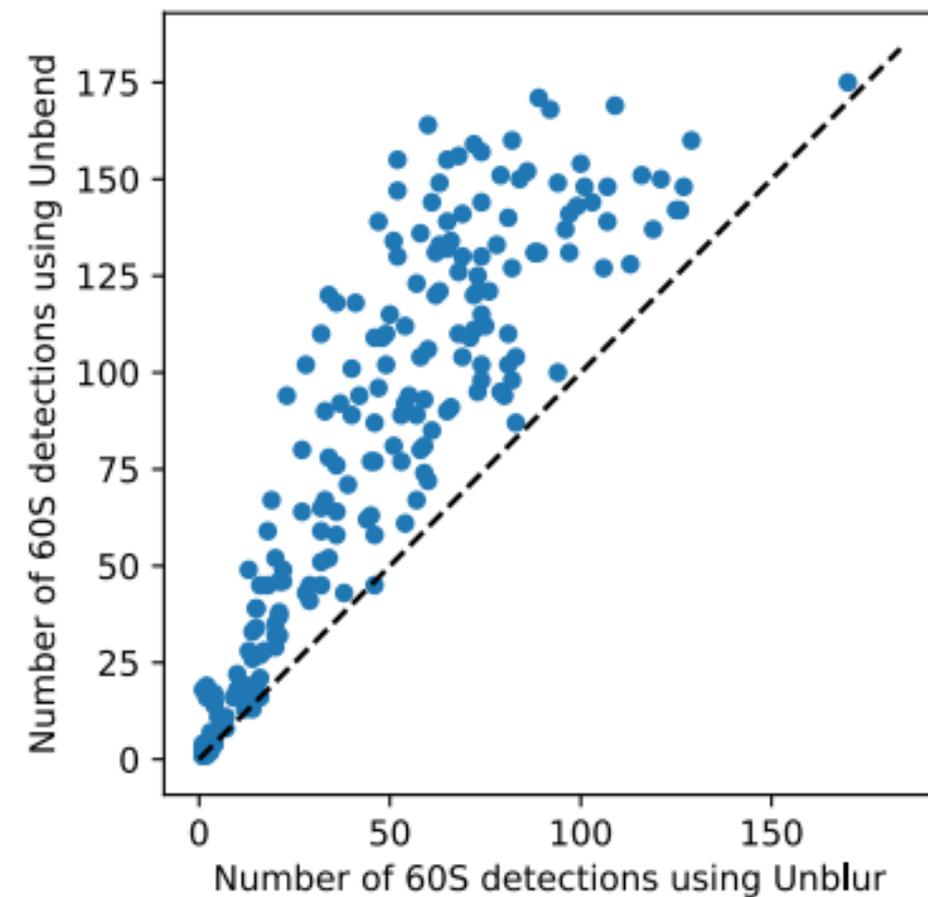
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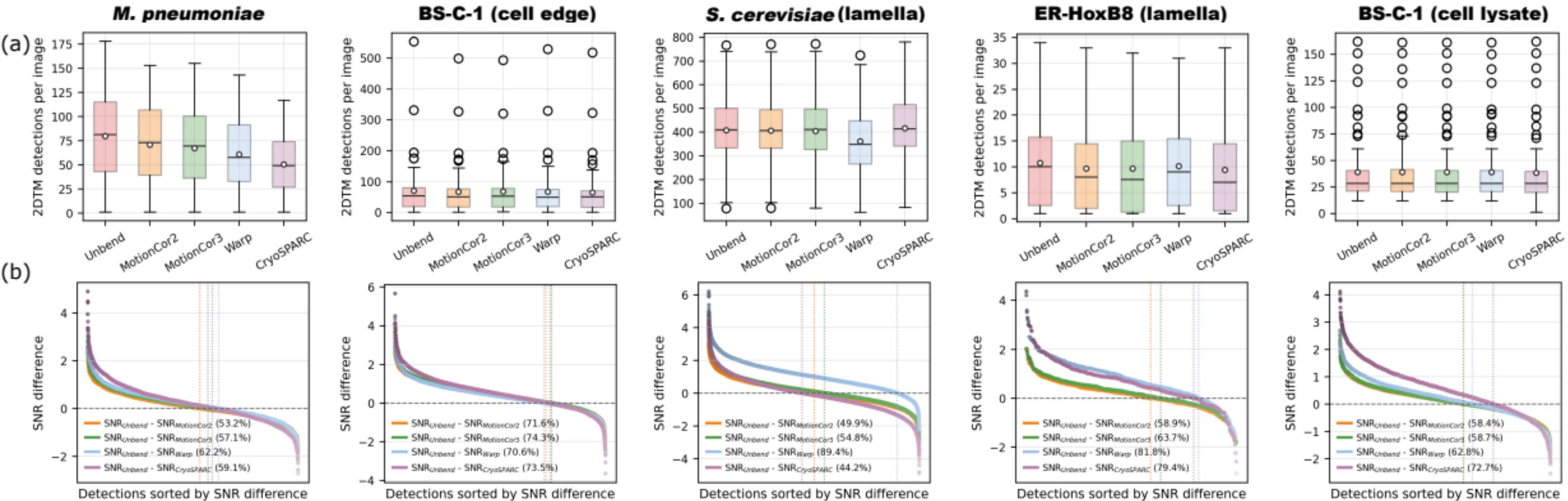


(b)



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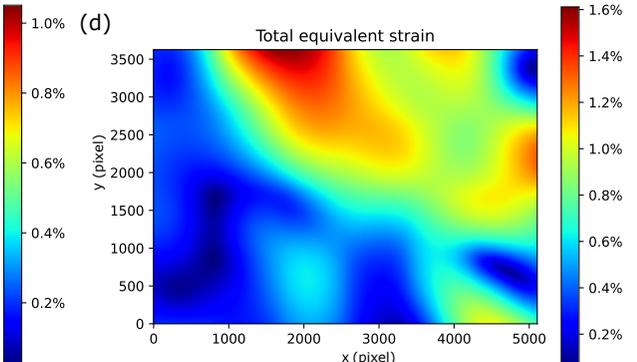
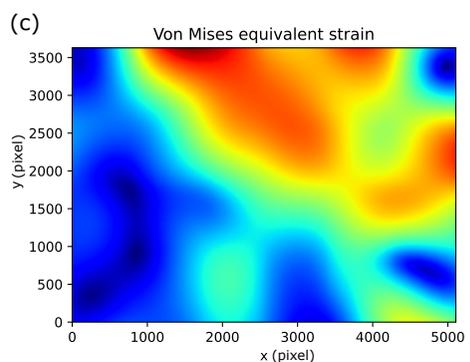
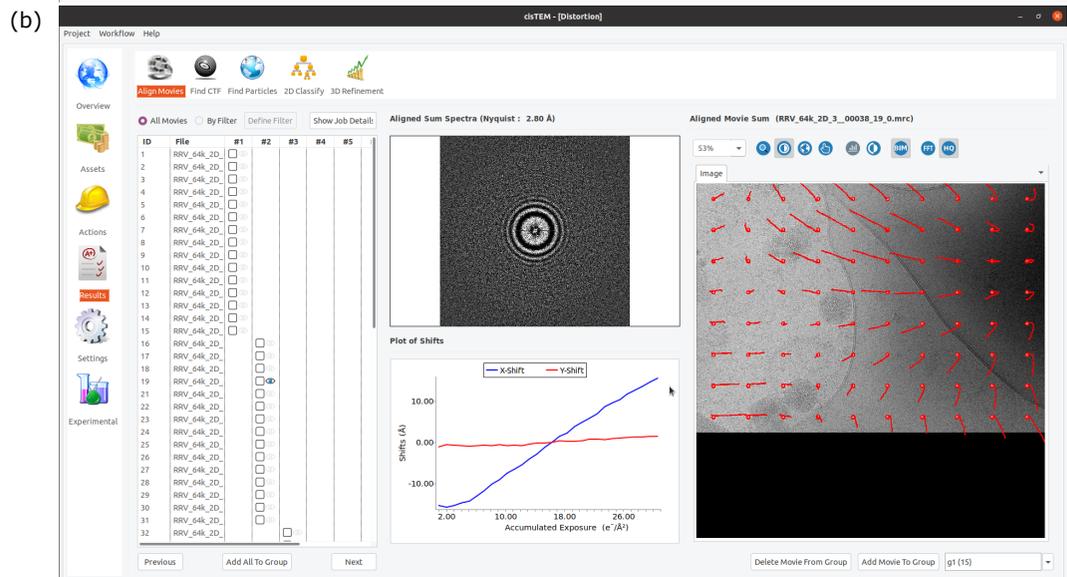
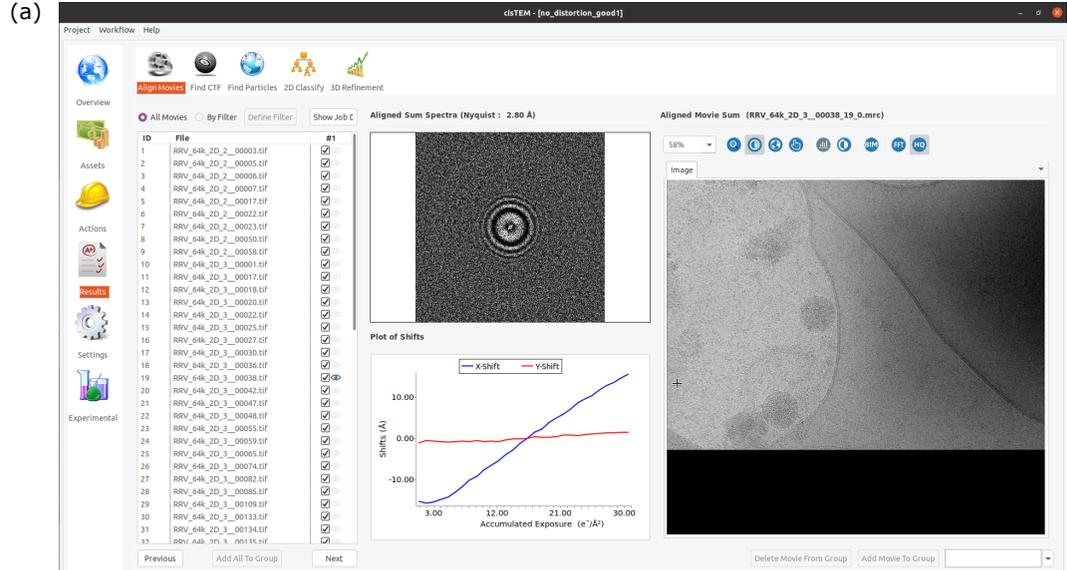


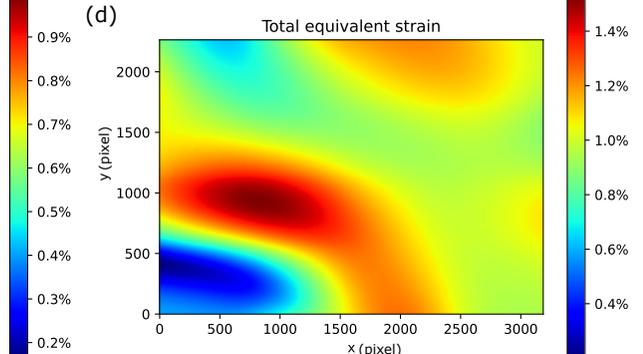
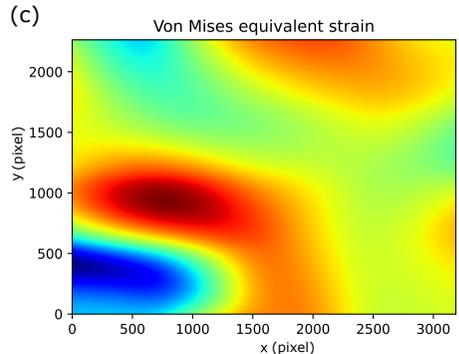
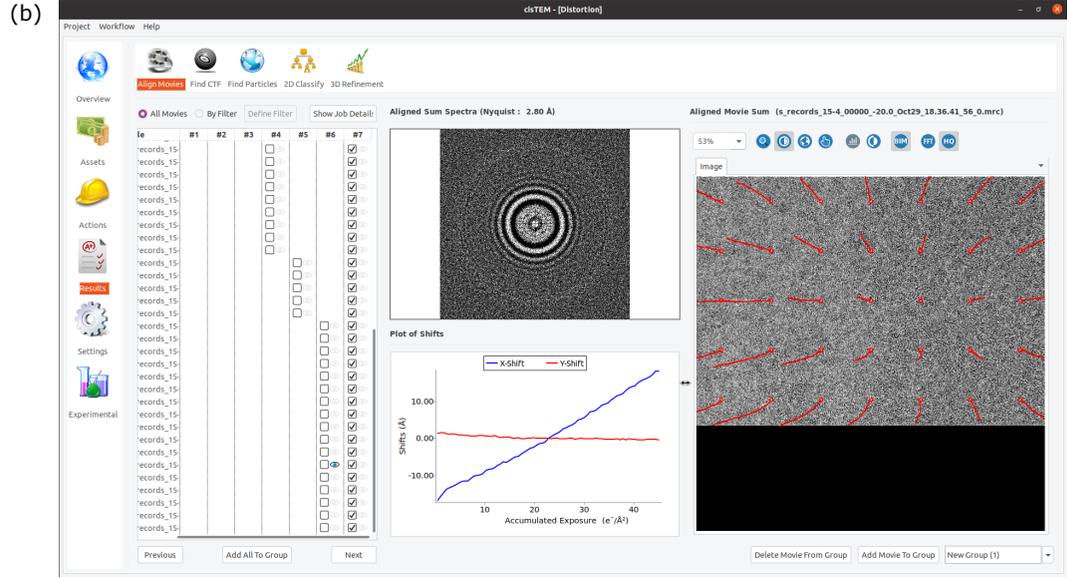
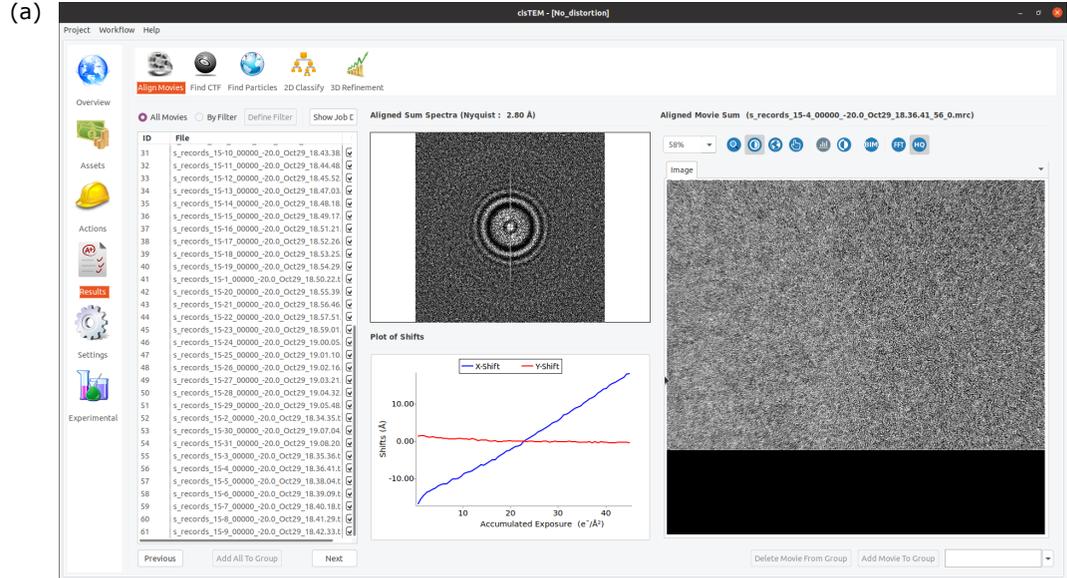
Algorithm S1 | Unbend movie alignment and local motion correction

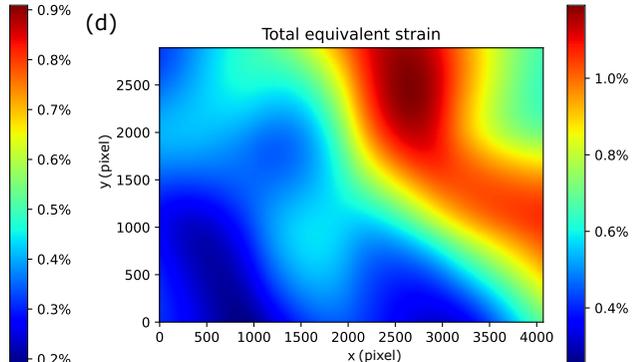
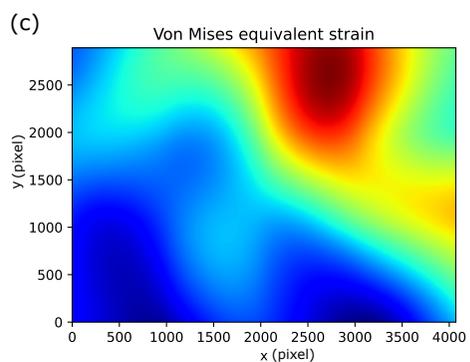
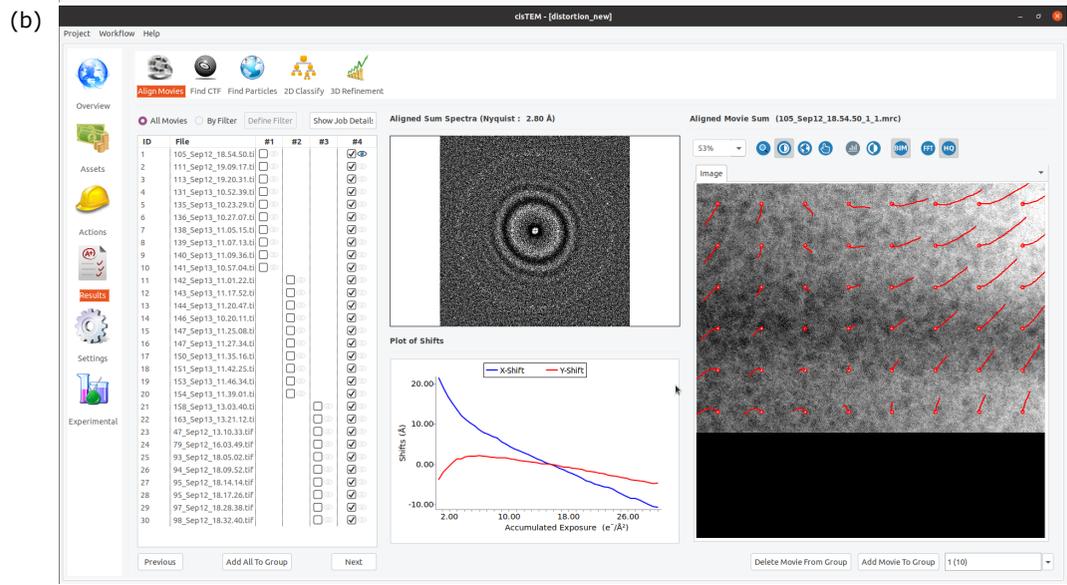
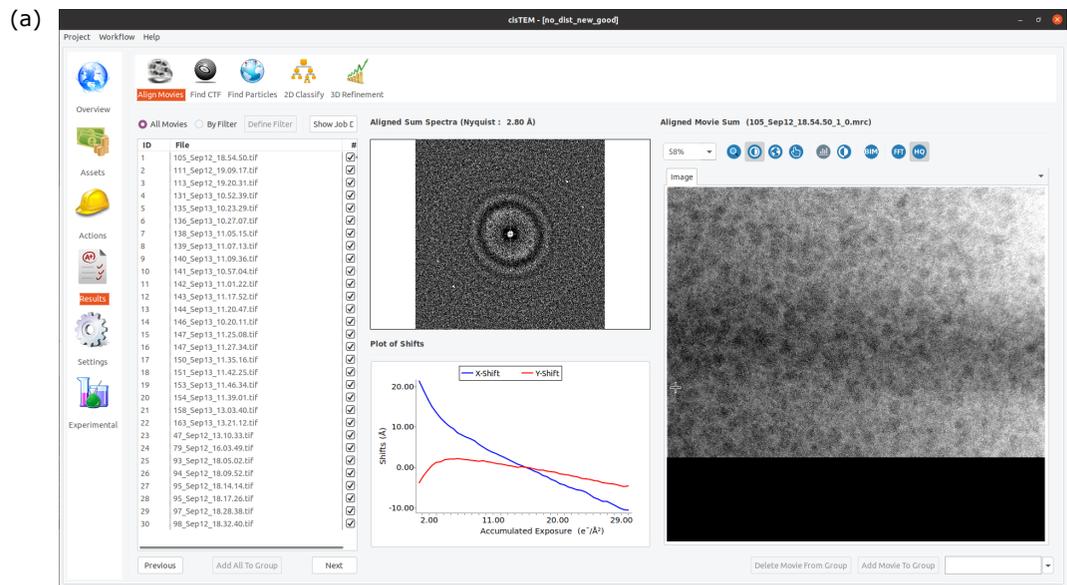
Input: Movie frames $\{I_f\}_{f=1}^{N_F}$ and movie frames metadata.

Output: Motion-corrected micrograph.

1. **Full-frame alignment:** Perform three-iteration global alignment (Unblur-style) with increasing resolution. Identify outlier frames by deviation from an SG reference trajectory ($>1.5 \times \text{IQR}$), re-align outliers with $2 \times B$ -factor, and retain raw shifts only if they remain outliers (see Full-frame alignment)
 2. **Patch trimming:** Choose patch size and patch grid (NP_x, NP_y) based on output pixel size or user settings; partition the globally aligned frames into patch stacks (see Patch alignment)
 3. **Patch-stack alignment:** For each patch, estimate per-frame shifts $\{(x_{i,f}, y_{i,f})\}$ by cross-correlation of each frame against the leave-one-out average of the remaining frames. (see Patch alignment)
 4. **Patch smoothing and repair:** Smooth each patch trajectory using an SG filter. Flag unreliable patches using inter-frame shift variability (Eqs. 1–2; $1.5 \times \text{IQR}$) and replace their shifts with those from the nearest-neighbor patch. (Patch alignment).
 5. **Spline model and knot grid:** Construct a 3D deformation model using bicubic B-splines in x – y and cubic B-splines along exposure/frame (z), with free-end boundary conditions. Set $(NK_x, NK_y) \approx \frac{2}{3}(NP_x, NP_y)$ (minimum 4), place z -knots every $4e^{-}/\text{\AA}^2$, and maintain knot parameters K_x and K_y . (see Sample distortion modeling and correction: knot grid configuration)
 6. **Initialize knots:** Fit (K_x, K_y) by minimizing the least-squares objective L_1 (Eq. 11). (see Sample distortion modeling and correction: Control points and knots)
 7. **Refine knots:** Refine (K_x, K_y) by minimizing the cross-correlation based objective L_2 using L-BFGS (Eqs. 12–13). (Sample distortion modeling and correction: Parameter refinement)
 8. **Warp and sum:** Evaluate pixel-wise shifts, warp frames (bilinear interpolation), pad/trim boundaries, and average corrected frames to generate the final micrograph. (see Sample distortion modeling and correction: Parameter refinement)
-







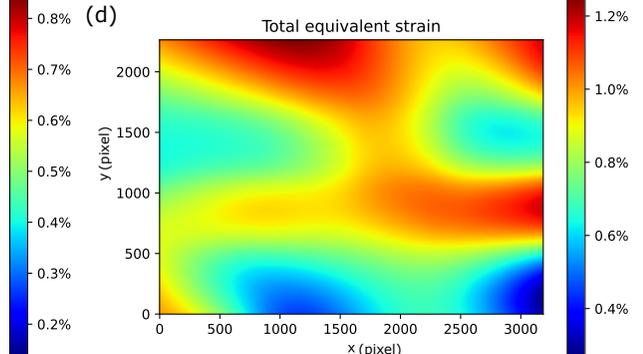
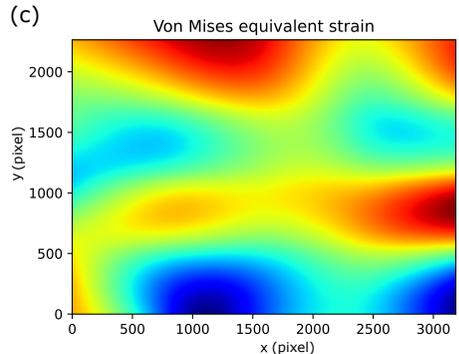
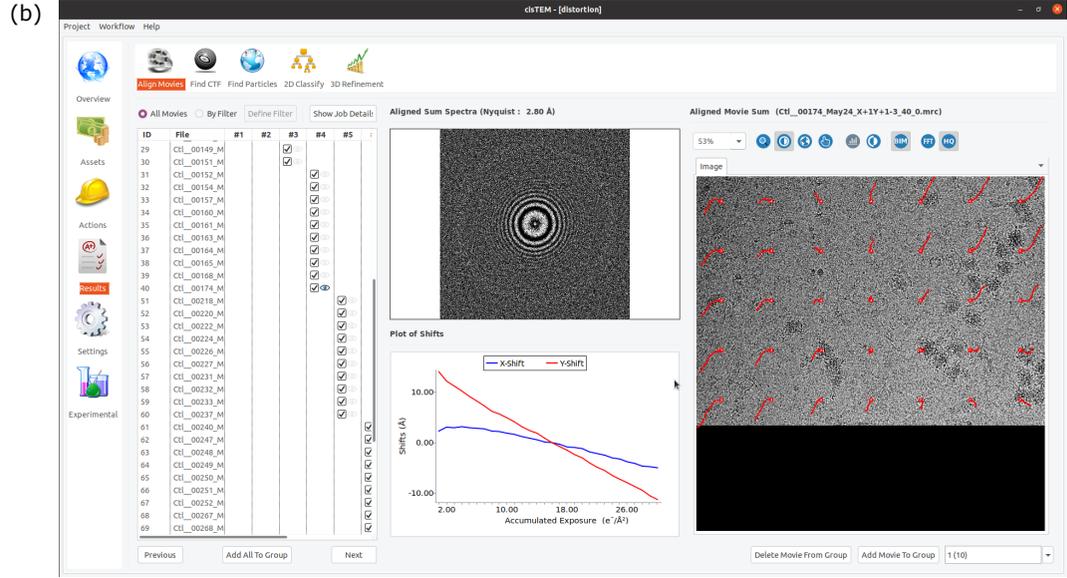
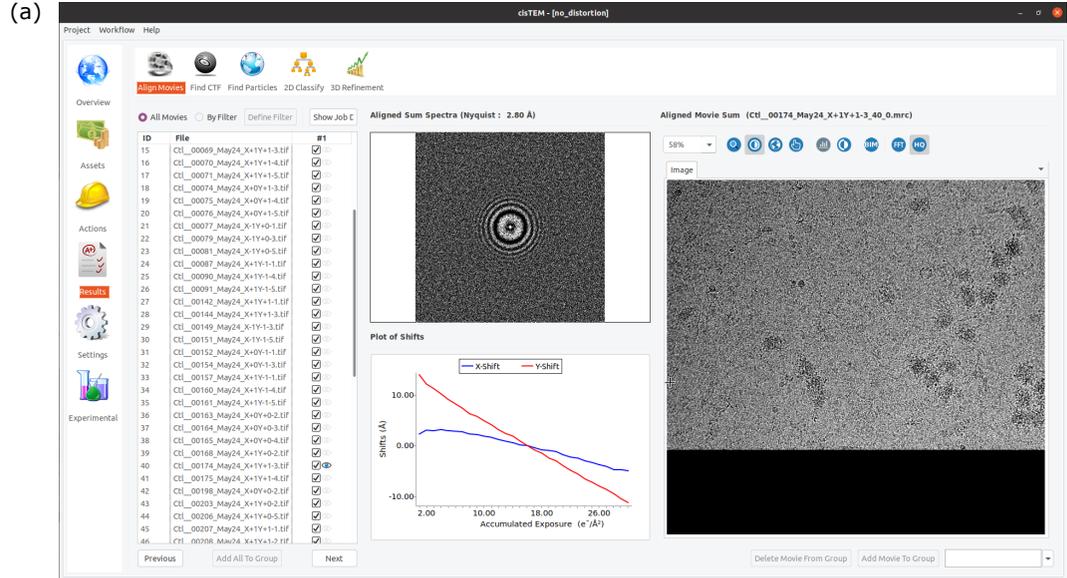


Figure 4—figure supplement 6 Motion and equivalent strain summary table for micrographs shown in Figure 4—figure supplements 1–5

	Max shift (Å)	Mean shift (Å)	Standard deviation (Å)	Von Mises equivalent strain	Total equivalent strain
M. pneumoniae	57.9	17.5	13.7	< 2.3%	< 3.5 %
C. aethiops: BS-C-1 (cell edge)	16.8	7.8	3.9	< 1.0 %	< 1.6 %
M. musculus: ER-HoxB8 lamellae	18.9	8.1	4.6	< 1.0 %	< 1.5 %
S. cerevisiae lamellae	13.2	5.3	3.6	< 0.9 %	< 1.2 %
C. aethiops: BS-C-1 (cell lysate)	9.1	3.4	2.3	< 0.8 %	< 1.2 %

For each micrograph, the mean patch shift was computed across patches; the table reports summary statistics of these per-micrograph means for each dataset.

Figure 4—figure supplement 7 Summary statistics of per-micrograph mean patch shifts by sample type.

Sample	Mean (Å)	Standard deviation (Å)	Min (Å)	Max (Å)	Median (Å)
M. pneumoniae	4.31	2.17	0.27	17.46	4.10
BS-C-1 (cell edge)	2.45	1.70	0.39	7.78	2.35
S. cerevisiae (lamella)	1.44	1.04	0.28	5.30	1.24
ER-HoxB8 (lamella)	2.48	1.68	0.50	8.10	2.04
BS-C-1 (cell lysate)	0.72	0.67	0.29	3.44	0.49

Figure 8—figure supplement 1

Statistics table for detected particles from micrographs processed by different software

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Method	2DTM SNR (mean)	2DTM SNR (median)	Detections per micrograph (mean)	Detections per micrograph (median)	Total detections	Common detections with Unbend	Fraction of overlap (Unbend having higher SNR) (%)	Fraction of overlap (Unbend having lower SNR) (%)	Fraction of overlap (Unbend having same SNR) (%)
Unbend	8.72	8.53	79.7	81.0	4864				
MotionCor2	8.70	8.52	70.6	73.0	4450	3793	53.2	46.1	0.7
MotionCor3	8.67	8.47	67.2	69.5	4167	3559	57.1	42.1	0.8
Warp	8.64	8.47	60.7	57.5	3761	3217	62.2	37.0	0.8
CryoSPARC	8.65	8.45	50.4	49.0	3025	2410	59.1	40.1	0.8
BS-C-1 (cell edge)									
Unbend	10.46	10.26	70.6	53.5	4521				
MotionCor2	10.18	9.98	67.8	50.5	4336	4191	71.6	28.1	0.4
MotionCor3	10.14	9.94	68.1	53.0	4293	4162	74.3	25.3	0.4
Warp	10.20	10.00	67.6	50.0	4324	4180	70.6	28.6	0.8
CryoSPARC	10.08	9.85	65.6	50.5	4197	3931	73.5	25.9	0.5
S. Cerevisiae (lamella)									
Unbend	10.65	10.51	407.4	408.5	12223				
MotionCor2	10.63	10.48	406.4	406.0	12192	11785	49.9	49.4	0.7
MotionCor3	10.52	10.40	404.1	411.0	12122	11741	54.8	44.6	0.6
Warp	9.85	9.66	361.4	347.5	10842	10664	89.4	10.4	0.2
CryoSPARC	10.69	10.56	415.6	413.5	12469	11436	44.2	55.4	0.5
ER-HoxB8 (lamella)									
Unbend	11.46	11.35	10.7	10.0	407				
MotionCor2	11.27	11.26	9.7	8.0	416	389	58.9	40.4	0.8
MotionCor3	11.30	11.23	9.7	7.5	406	388	63.7	35.8	0.5
Warp	10.82	10.83	10.1	9.0	395	369	81.8	17.6	0.5
CryoSPARC	10.84	10.74	9.4	7.0	405	345	79.4	20.3	0.3
BS-C-1 (cell lysate)									
Unbend	14.24	14.43	38.8	28.0	2910				
MotionCor2	14.12	14.30	38.8	28.0	2909	2892	58.4	40.5	1.0
MotionCor3	14.11	14.28	38.8	28.0	2911	2890	58.7	40.6	0.8
Warp	14.02	14.21	38.8	28.0	2909	2887	62.8	36.7	0.5
CryoSPARC	13.71	13.93	38.1	28.0	2899	2875	72.7	26.9	0.5